

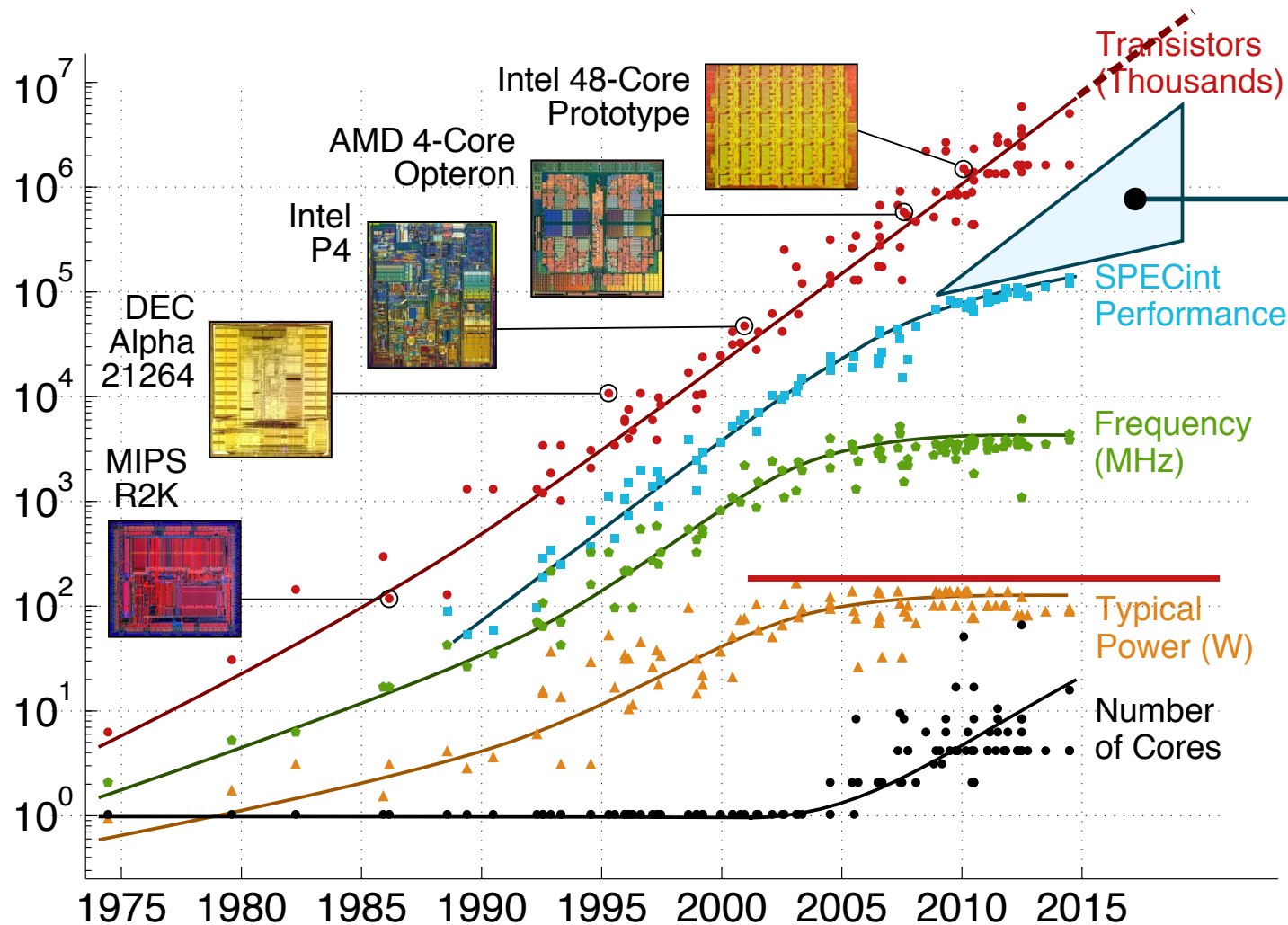
Architectural Specialization for Inter-Iteration Loop Dependence Patterns

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Cornell University

Fall 2015

Motivating Trends in Computer Architecture



Data collected by M. Horowitz, F. Labonte, O. Shacham, K. Olukotun, L. Hammond, C. Batten

Hardware Specialization

Data-Parallelism via GPGPUs and Vector

Fine-Grain Task-Level Parallelism

Instruction Set Specialization

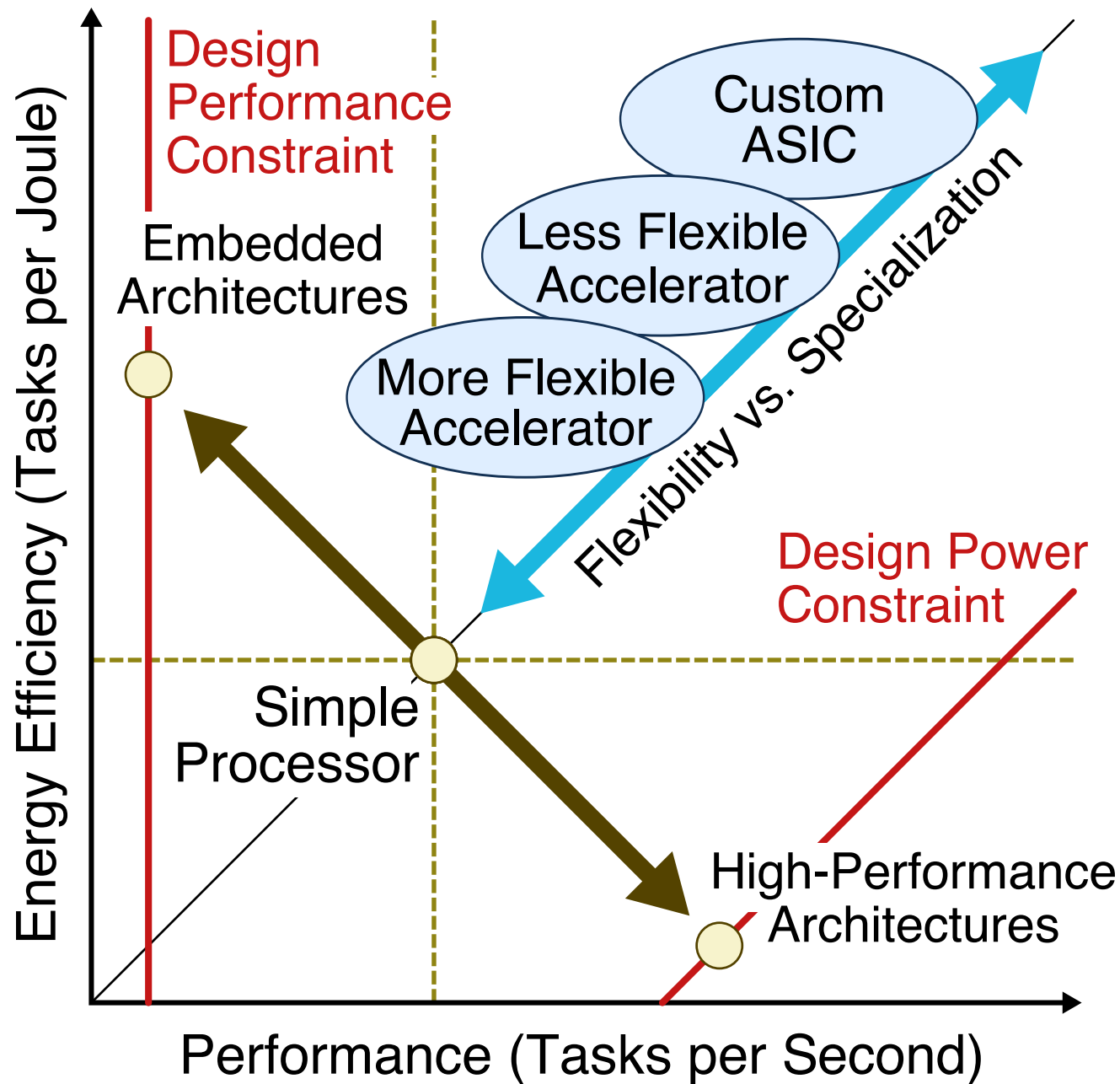
Subgraph Specialization

Application-Specific Accelerators

Domain-Specific Accelerators

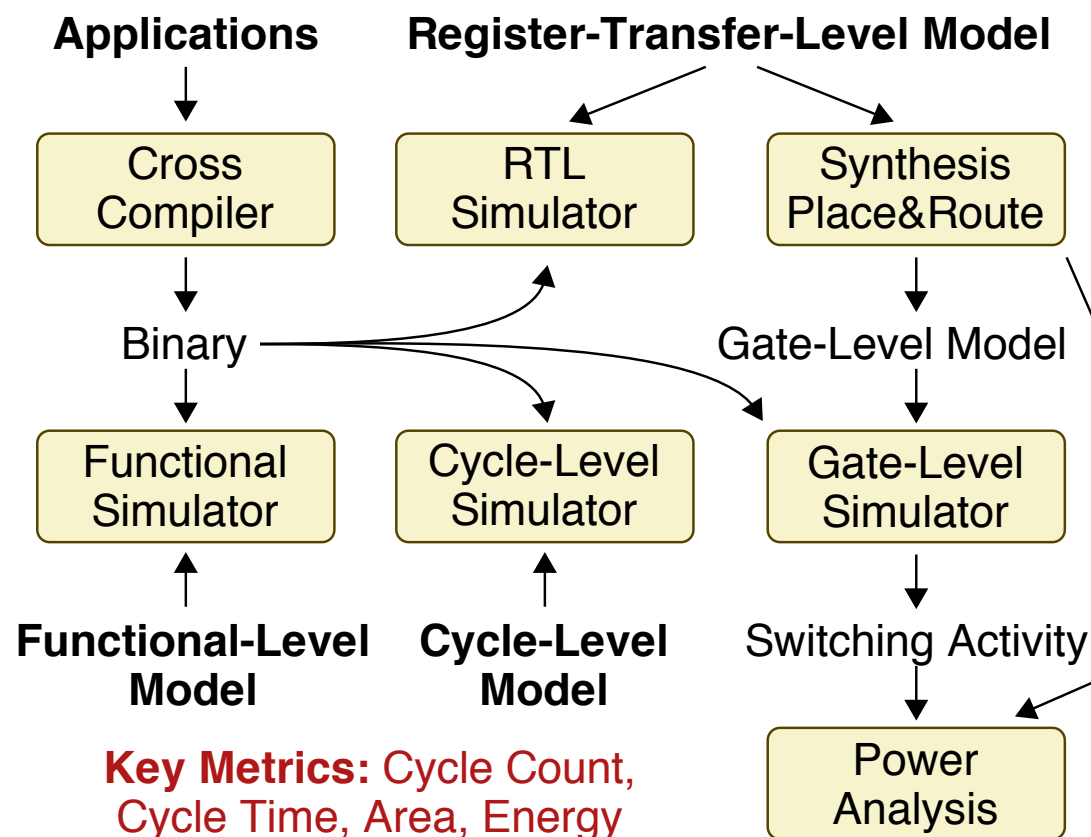
Coarse-Grain Reconfig Arrays

Field-Programmable Gate Arrays



Vertically Integrated Research Methodology

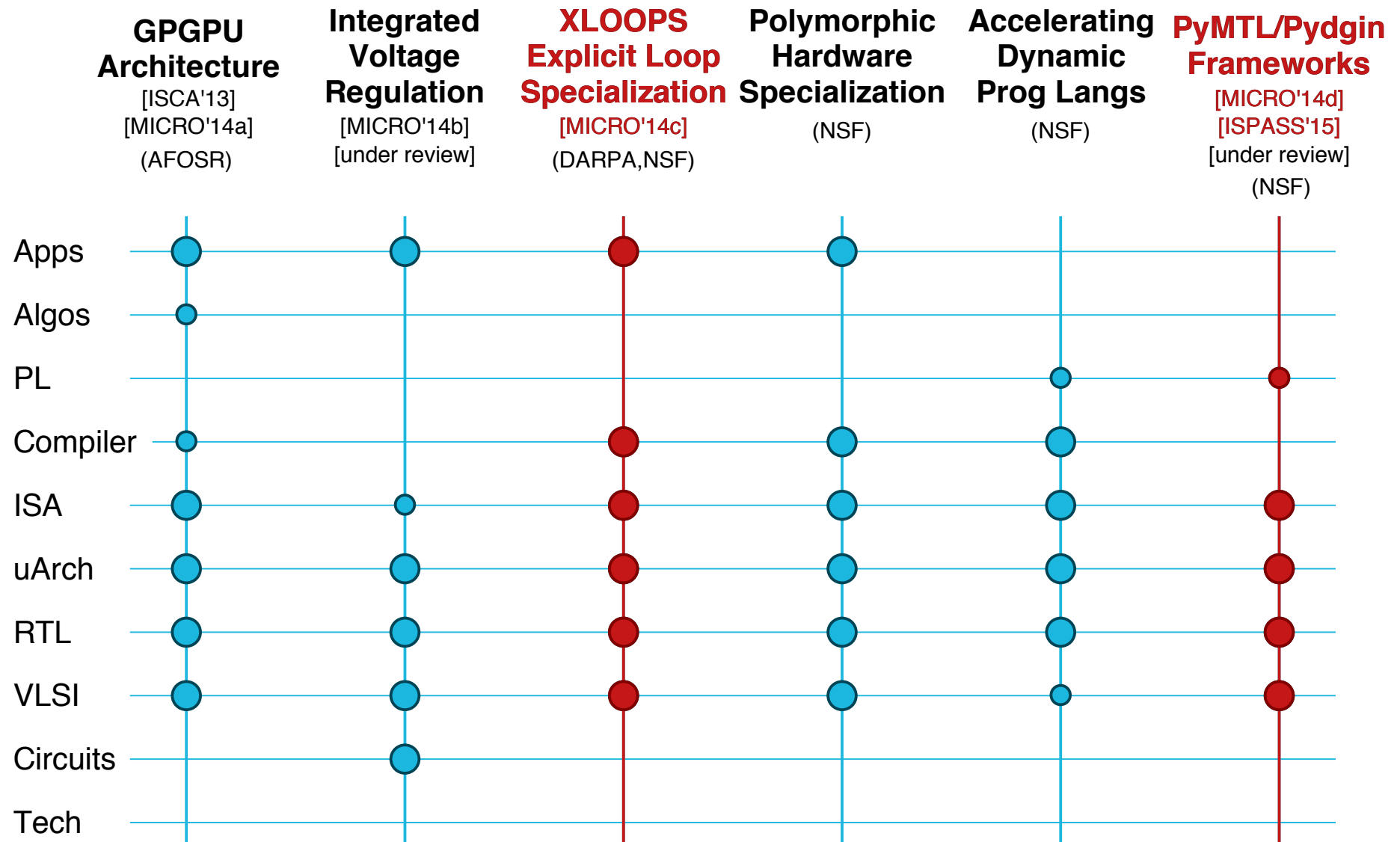
Our research involves reconsidering all aspects of the computing stack including applications, programming frameworks, compiler optimizations, runtime systems, instruction set design, microarchitecture design, VLSI implementation, and hardware design methodologies



Experimenting with full-chip layout, FPGA prototypes, and test chips is a key part of our research methodology



Projects Within the Batten Research Group

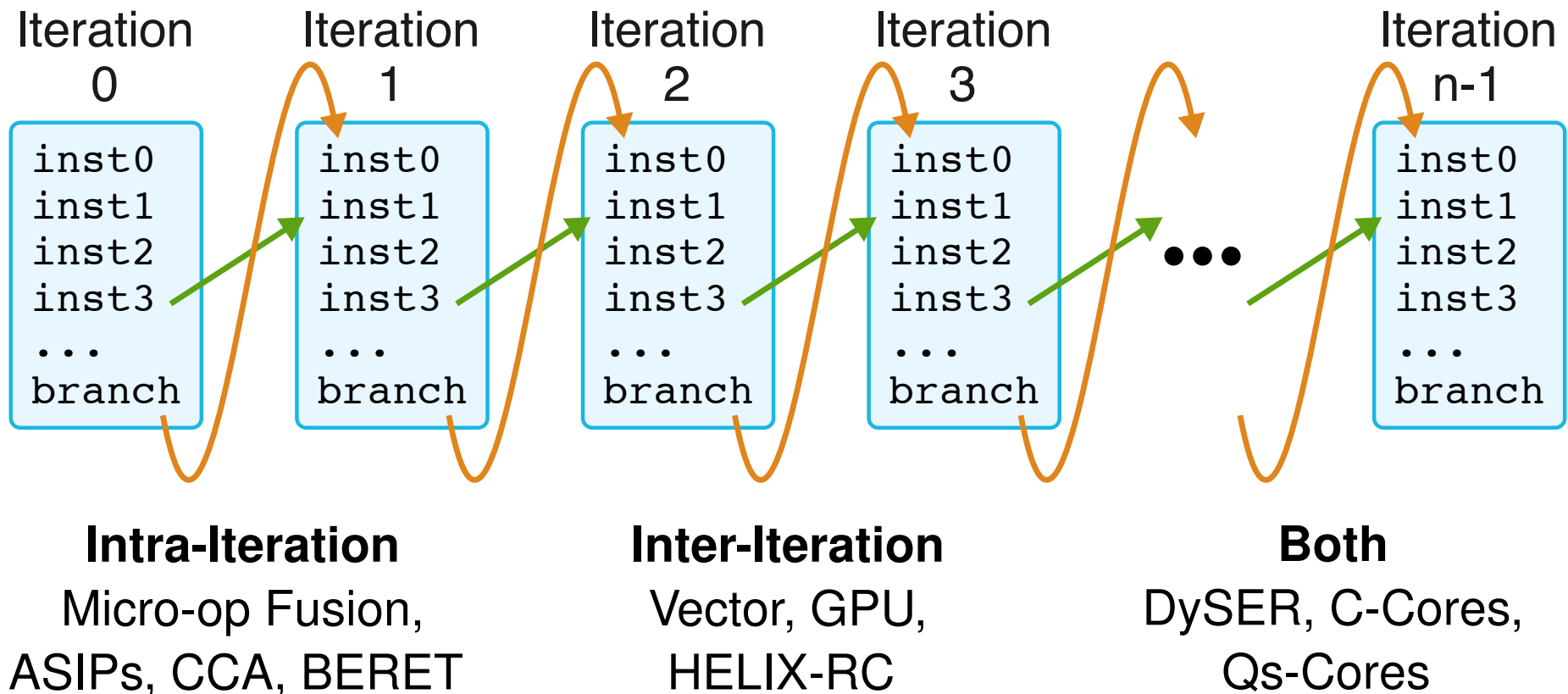


XLOOPS: Architectural Specialization for Inter-Iteration Loop Dependence Patterns

Shreesha Srinath, Berkin Ilbeyi, Mingxing Tan, Gai Liu,
Zhiru Zhang, and Christopher Batten

47th ACM/IEEE Int'l Symp. on Microarchitecture (MICRO)
Cambridge, UK, Dec. 2014

Loop Dependence Pattern Specialization

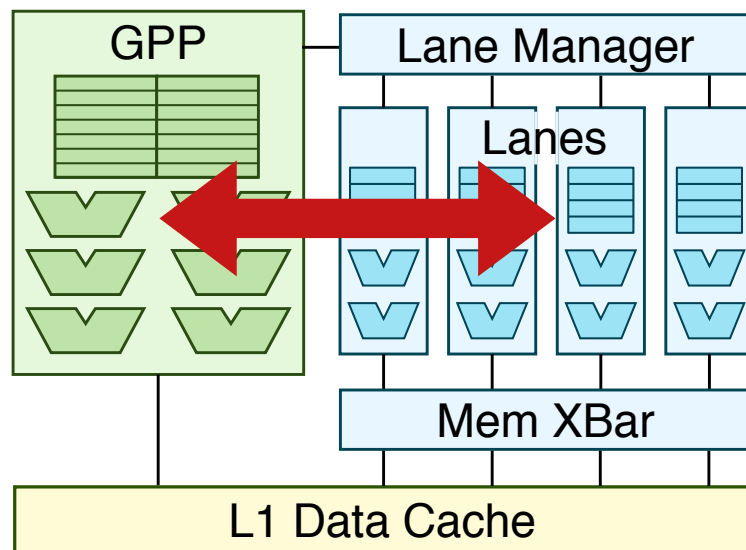


Key Challenge: Creating HW/SW abstractions that are flexible and enable performance-portable execution

Explicit Loop Specialization (XLOOPS)

Key Idea 1: Expose fine-grained parallelism by elegantly encoding inter-iteration loop dependence patterns in the ISA

Key Idea 2: Single-ISA heterogeneous architecture with a new execution paradigm supporting traditional, specialized, and adaptive execution



- ▶ **Traditional Execution**
- ▶ **Specialized Execution**
- ▶ **Adaptive Execution**

1. XLOOPS Instruction Set

loop:

lw r2, 0(rA)

lw r3, 0(rB)

...

addiu.xi rA, 4

addiu.xi rB, 4

addiu r1, r1, 1

xloop.uc r1, rN, loop

2. XLOOPS Compiler

#pragma xloops ordered

for(i = 0; i < N; i++)

A[i] = A[i] * A[i-K];

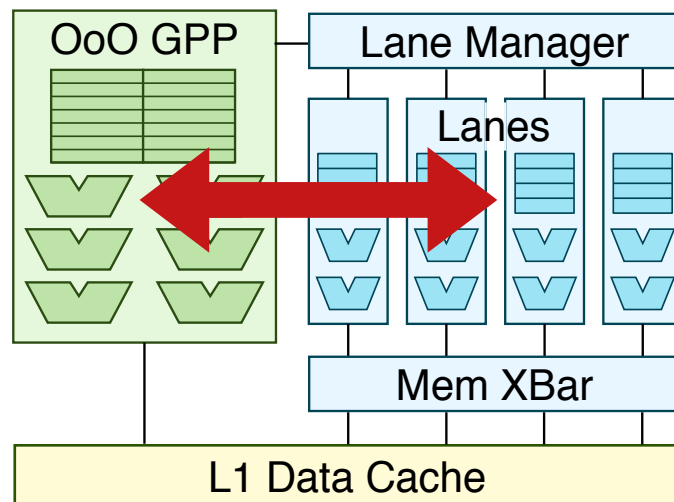
#pragma xloops atomic

for(i = 0; i < N; i++)

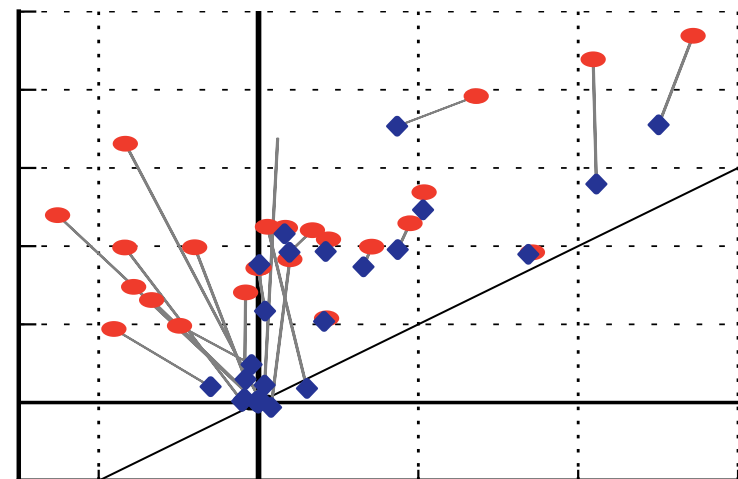
B[A[i]]++;

D[C[i]]++;

3. XLOOPS Microarchitecture



4. Evaluation



1. XLOOPS Instruction Set

loop:

```
lw      r2, 0(rA)
```

```
lw      r3, 0(rB)
```

```
...
```

```
addiu.xi rA, 4
```

```
addiu.xi rB, 4
```

```
addiu    r1, r1, 1
```

```
xloop.uc r1, rN, loop
```

2. XLOOPS Compiler

```
#pragma xloops ordered
```

```
for(i = 0; i < N i++)
```

```
    A[i] = A[i] * A[i-K];
```

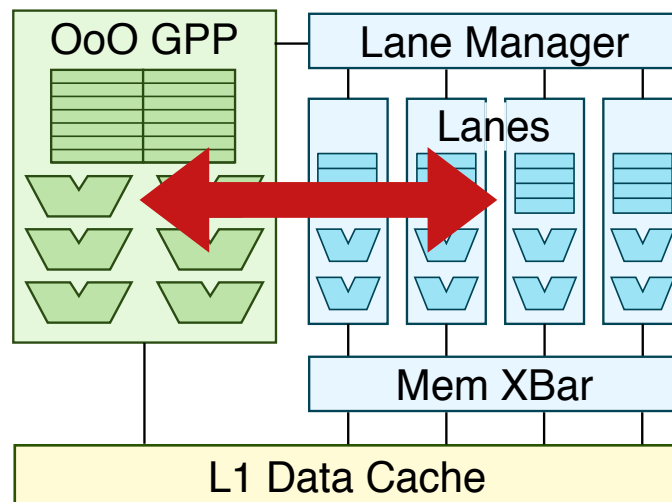
```
#pragma xloops atomic
```

```
for(i = 0; i < N; i++)
```

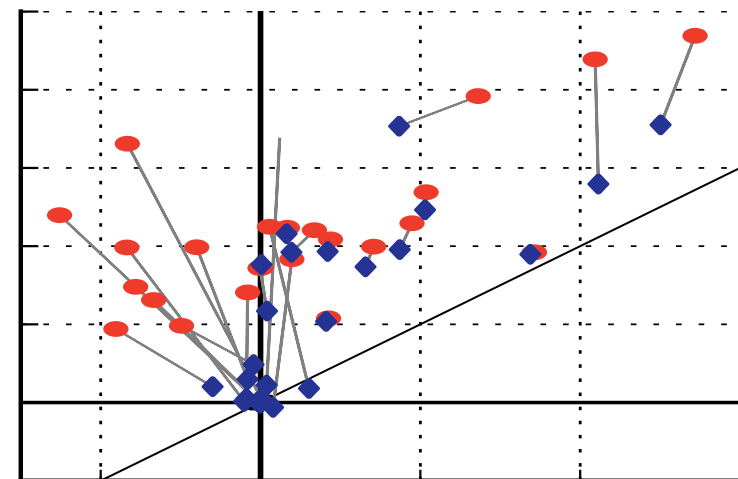
```
    B[ A[i] ]++;
```

```
    D[ C[i] ]++;
```

3. XLOOPS Microarchitecture



4. Evaluation

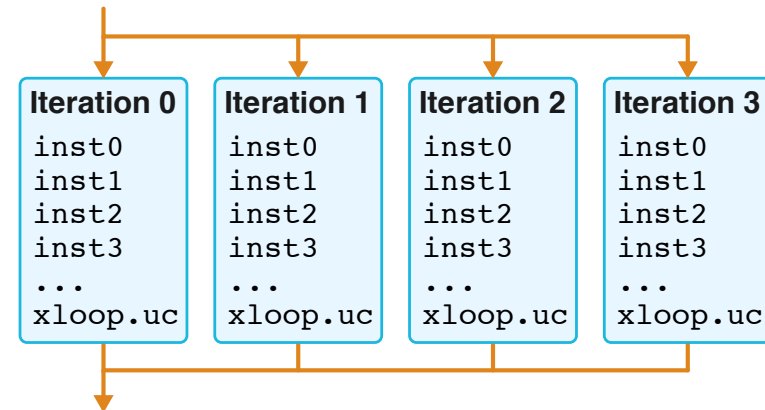


XLOOPS Instruction Set: Unordered Concurrent

Element-wise Vector Multiplication

```
for ( i=0; i<N; i++ )
    C[i] = A[i] * B[i]
```

```
loop:
    lw      r2, 0(rA)
    lw      r3, 0(rB)
    mul     r4, r2, r3
    sw      r4, 0(rC)
    addiu.xi rA, 4
    addiu.xi rB, 4
    addiu.xi rC, 4
    addiu    r1, r1, 1
    xloop.uc r1, rN, loop
```



- ▶ Instructions in loop cannot write live-in registers
- ▶ Live-out values must be stored to memory
- ▶ Data-races are possible

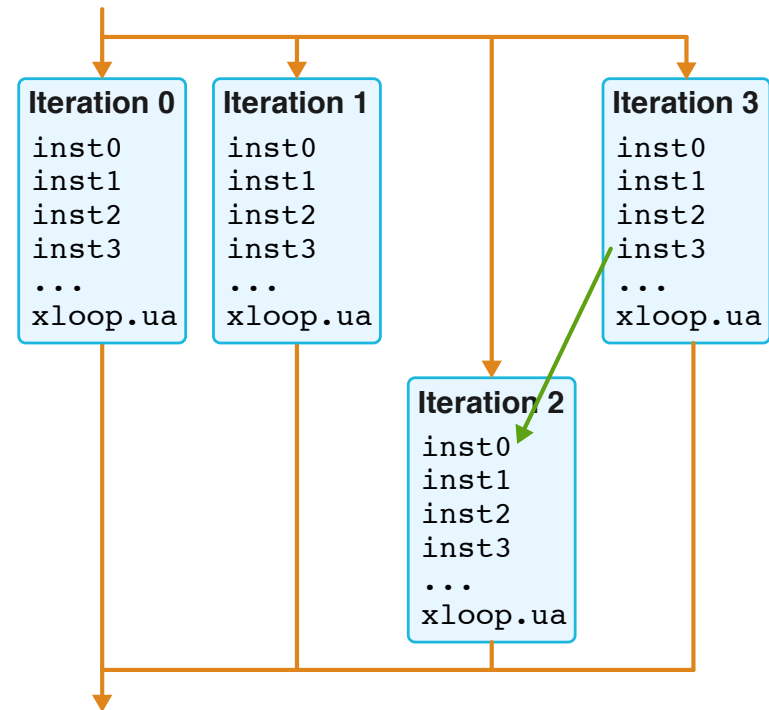
XLOOPS Instruction Set: Unordered Atomic

Histogram Updates

```

for ( i=0; i<N; i++ )
    B[A[i]]++; D[C[i]]++;

loop:
    lw        r6, 0(rA)
    lw        r7, 0(r6)
    addiu     r7, r7, 1
    sw        r7, 0(r6)
    addiu.xi  rA, 4
    ...
    addiu     r1, r1, 1
    xloop.ua  r1, rN, loop
  
```



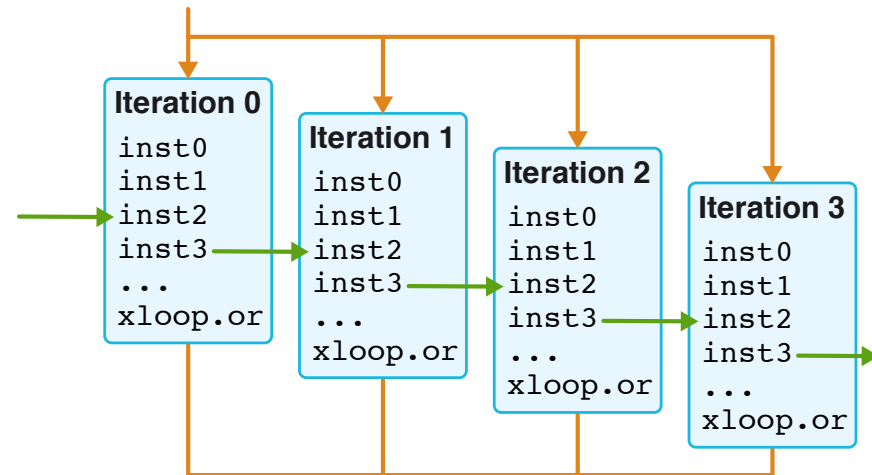
- Iterations execute atomically
- No race conditions
- Results can be non-deterministic
- Inspired by Transactional Memory

XLOOPS Instruction Set: Ordered-Through-Registers

Parallel-Prefix Summation

```
for ( i=0; i<N; i++ )
    X += A[i]; B[i] = X
```

```
loop:
    lw        r2, 0(rA)
    addu      rX, r2, rX
    sw        rX, 0(rB)
    addiu.xi  rA, 4
    addiu.xi  rB, 4
    addiu     r1, r1, 1
    xloop.or  r1, rN, loop
```



- **rX** - Cross Iteration Register
- CIRs are guaranteed to have the same value as a serial execution
- Inspired by Multiscalar

XLOOPS Instruction Set: Ordered-Through-Memory

```
for ( i=k; i<N; i++ )
    A[i] = A[i] * A[i-k];
```

```
# r1 = rK
```

```
# r3 = rA + 4*rK
```

```
loop:
```

```
    lw        r4, 0(r3)
```

```
    lw        r5, 0(rA)
```

```
    mul       r6, r4, r5
```

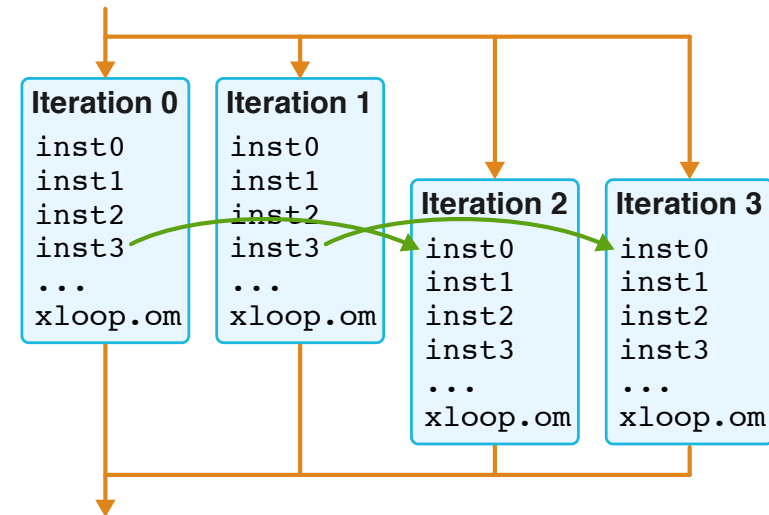
```
    sw        r6, 0(r3)
```

```
    addiu.xi  r3, 4
```

```
    addiu.xi  rA, 4
```

```
    addiu     r1, r1, 1
```

```
    xloop.om  r1, rN, loop
```

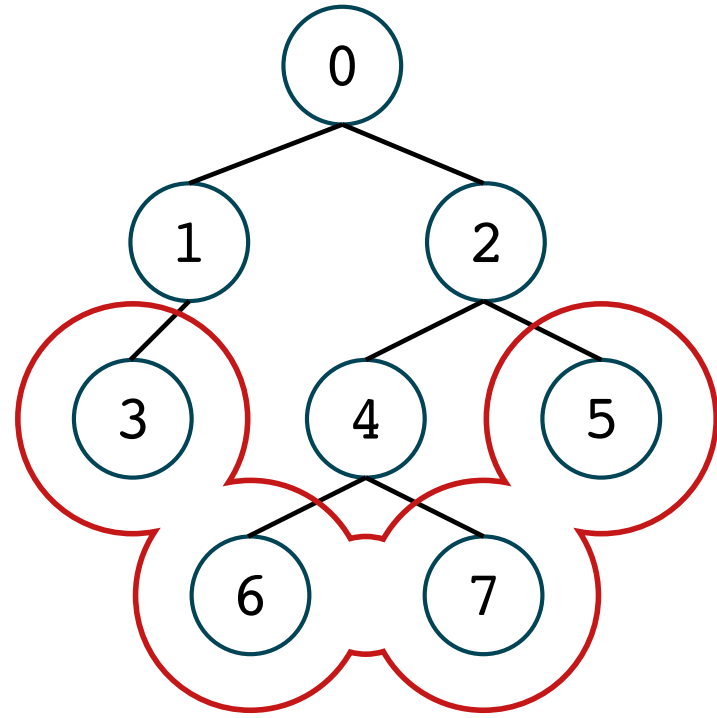
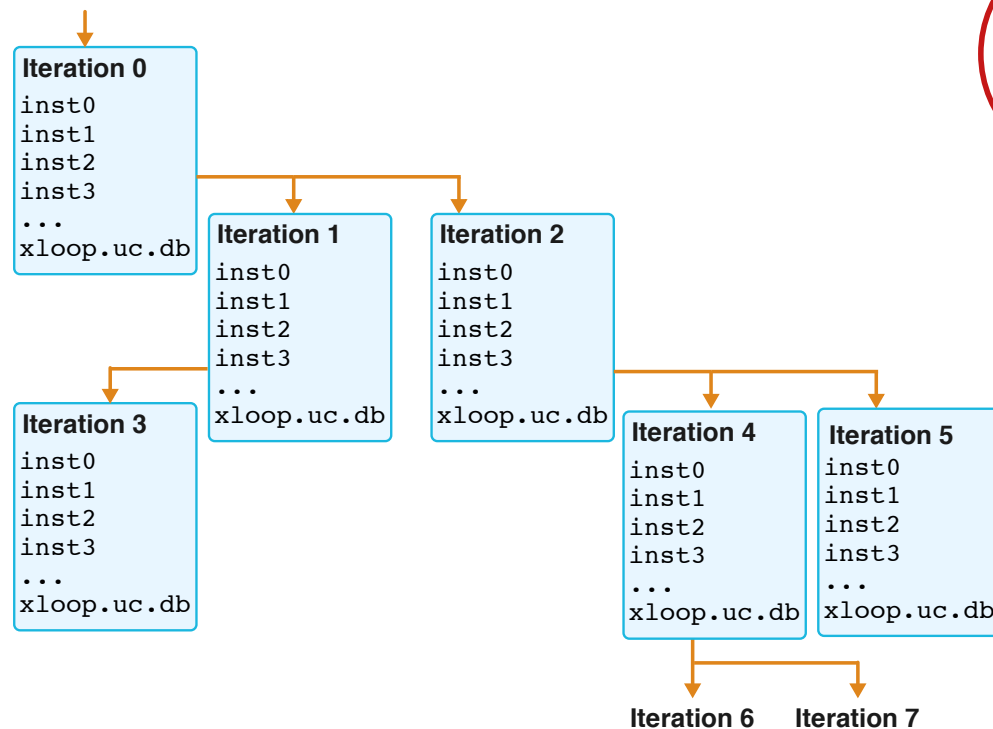


- Updates to memory defined by serial iteration order
- No race conditions
- Inspired by Multiscalar, TLS

XLOOPS Instruction Set: Dynamic Bound

- Parallelize using `xloop.uc.db`

```
for ( i=0; i<N; i++ )  
  ...  
  if ( cond ) N++;
```



1. XLOOPS Instruction Set

loop:

```
lw      r2, 0(rA)
```

```
lw      r3, 0(rB)
```

```
...
```

```
addiu.xi rA, 4
```

```
addiu.xi rB, 4
```

```
addiu    r1, r1, 1
```

```
xloop.uc r1, rN, loop
```

2. XLOOPS Compiler

```
#pragma xloops ordered
```

```
for(i = 0; i < N i++)
```

```
    A[i] = A[i] * A[i-K];
```

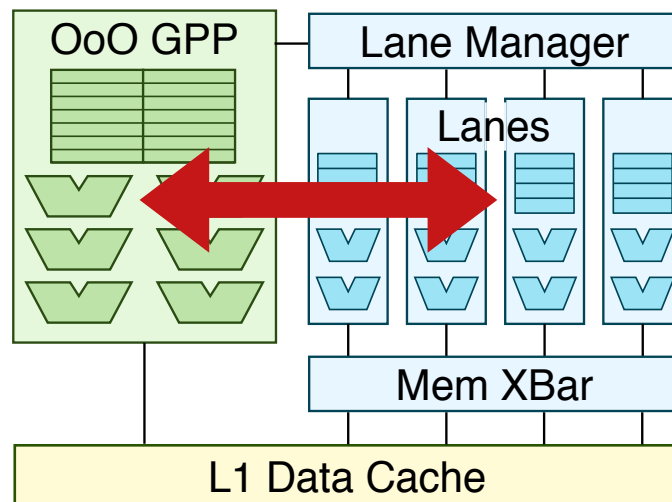
```
#pragma xloops atomic
```

```
for(i = 0; i < N; i++)
```

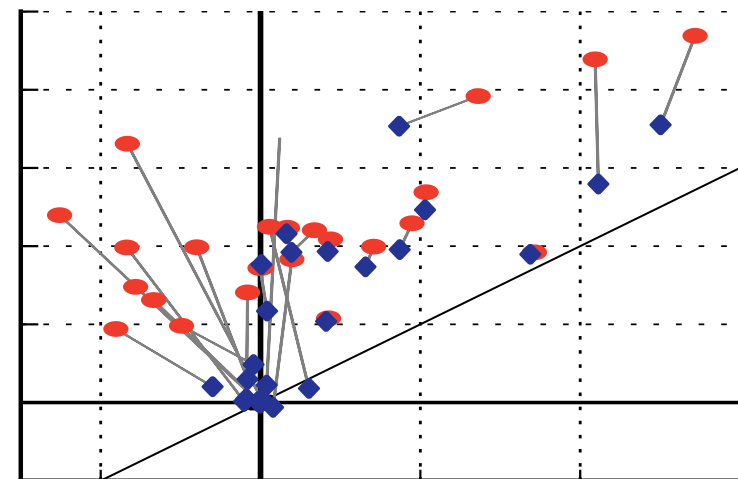
```
    B[ A[i] ]++;
```

```
    D[ C[i] ]++;
```

3. XLOOPS Microarchitecture



4. Evaluation



XLOOPS Compiler

Kernel implementing Floyd-Warshall shortest path algorithm

```
for ( int k = 0; k < n; k++ )
```

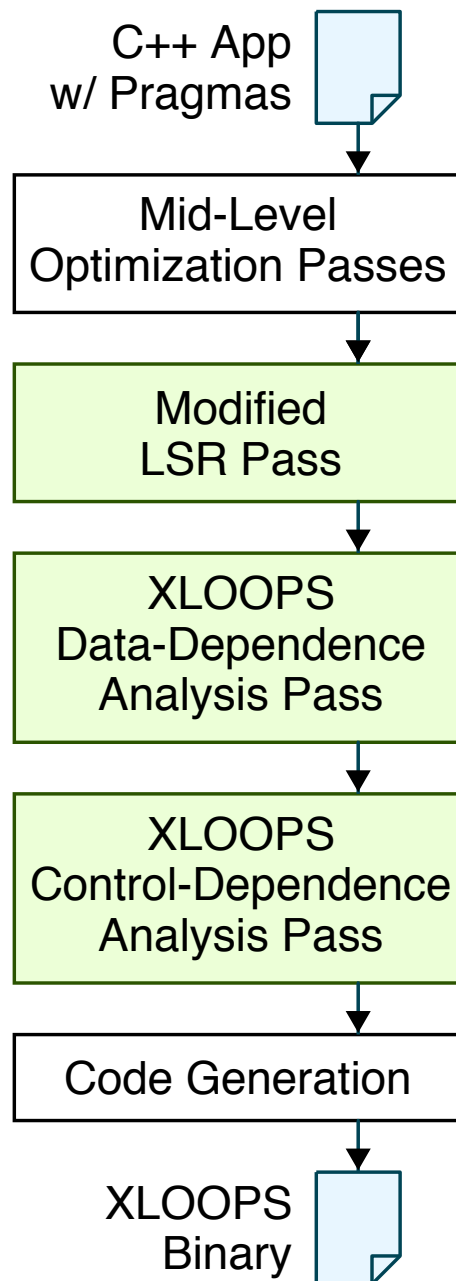
```
    #pragma xloops ordered
```

```
    for ( int i = 0; i < n; i++ )
```

```
        #pragma xloops unordered
```

```
        for ( int j = 0; j < n; j++ )
```

```
            path[i][j] = min( path[i][j], path[i][k] + path[k][j] );
```



▶ Programmer annotations

- ▷ unordered: no data-dependences
- ▷ ordered: preserve data-dependences
- ▷ atomic: atomic memory updates

▶ Loop strength reduction pass encodes MIVs as `xi` instructions

▶ XLOOPS data-dependence analysis pass

- ▷ Register-dependence: analysing use-definition chains through PHI nodes
- ▷ Memory-dependence: well known dependence analysis techniques

▶ Detect updates to the loop bound to encode dynamic-bound control-dependence pattern

1. XLOOPS Instruction Set

loop:

```
lw      r2, 0(rA)
```

```
lw      r3, 0(rB)
```

...

```
addiu.xi rA, 4
```

```
addiu.xi rB, 4
```

```
addiu    r1, r1, 1
```

```
xloop.uc r1, rN, loop
```

2. XLOOPS Compiler

```
#pragma xloops ordered
```

```
for(i = 0; i < N i++)
```

```
    A[i] = A[i] * A[i-K];
```

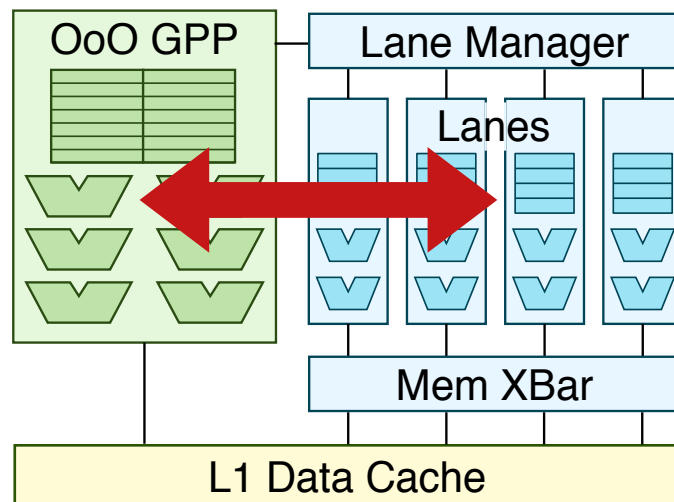
```
#pragma xloops atomic
```

```
for(i = 0; i < N; i++)
```

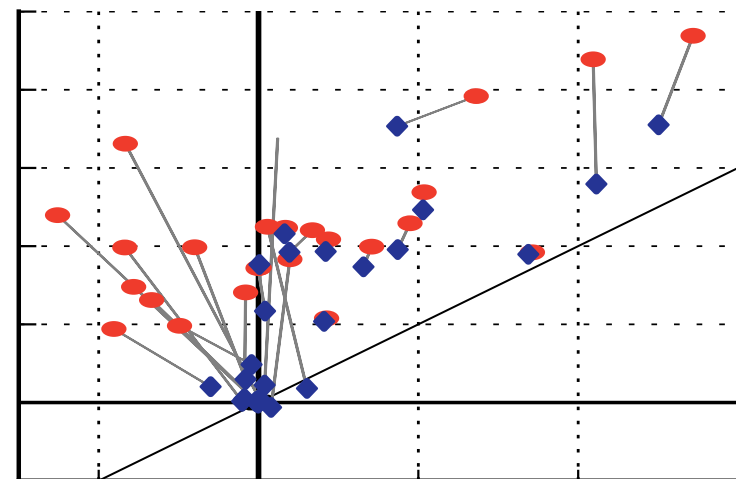
```
    B[ A[i] ]++;
```

```
    D[ C[i] ]++;
```

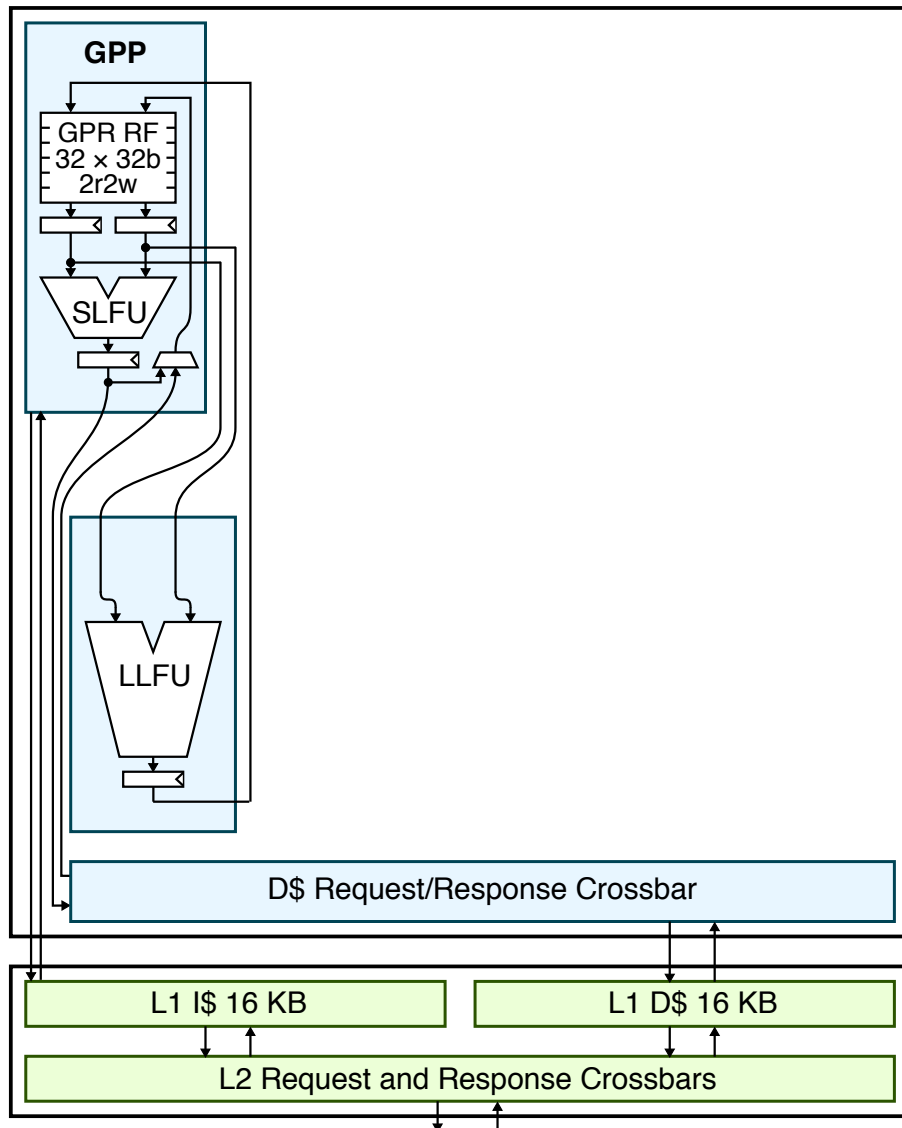
3. XLOOPS Microarchitecture



4. Evaluation



Traditional Execution



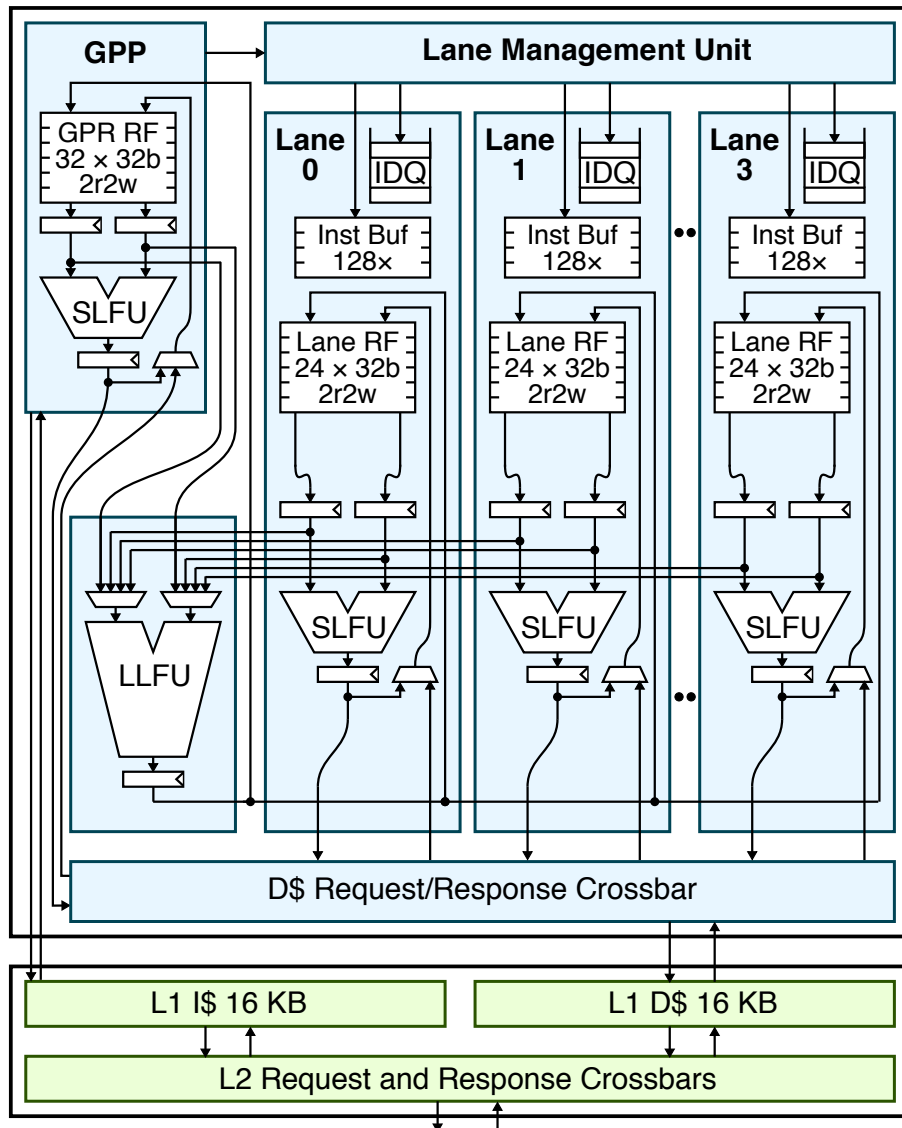
Minimal changes to a general-purpose processor (GPP)

- ▶ `xloop` → `bne`
- ▶ `addiu.xi` → `addiu`
- ▶ `addu.xi` → `addu`

Efficient traditional execution

- ▶ Enables gradual adoption
- ▶ Enables adaptive execution to migrate an `xloop` instruction

Specialized Execution – xloop.uc



Loop Pattern Specialization Unit

- ▶ Lane Management Unit (LMU)
- ▶ Four decoupled in-order lanes
- ▶ Lanes contain instruction buffers and index queues
- ▶ Lanes and the GPP arbitrate for data-memory port and long-latency functional unit

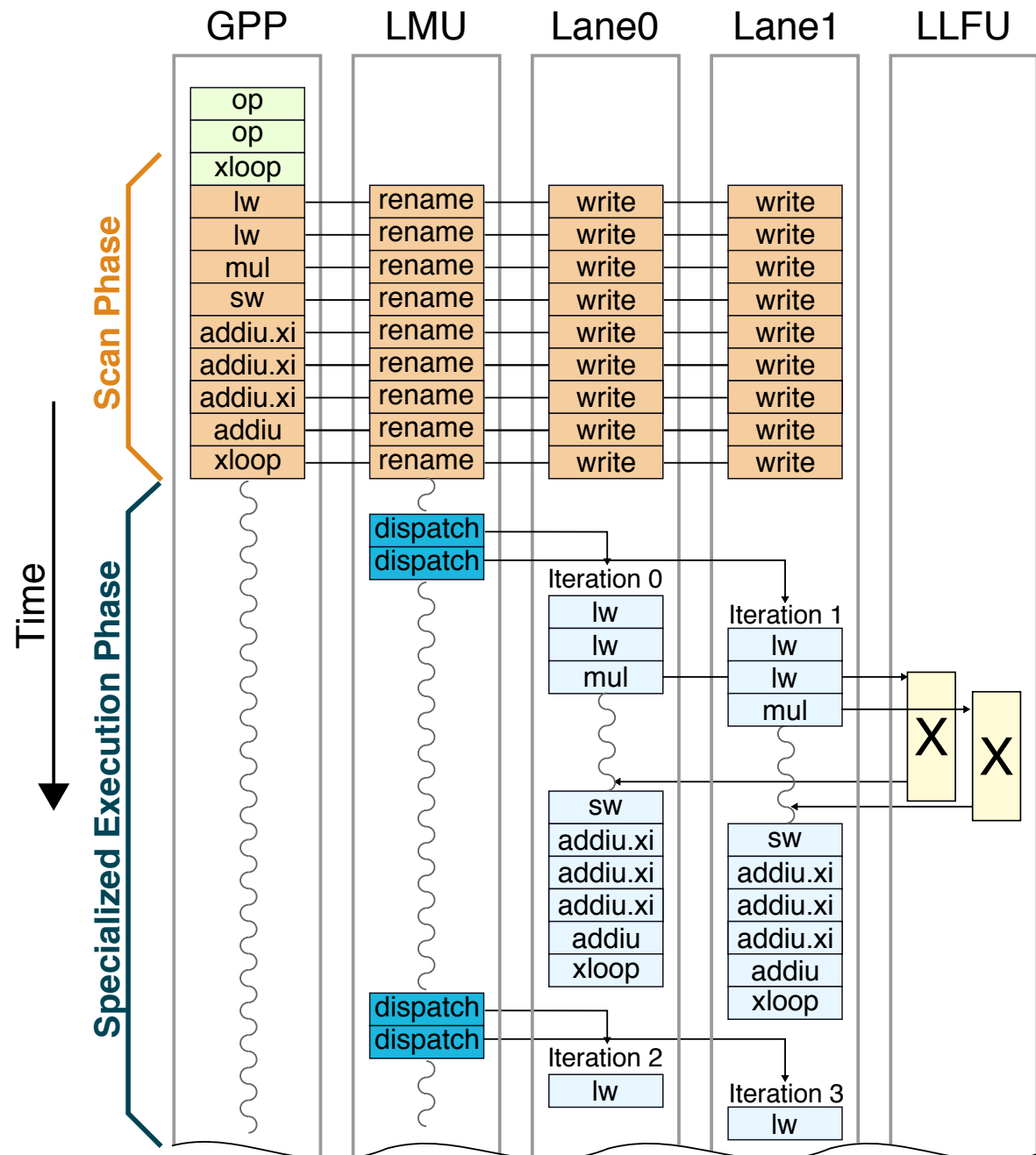
Specialized execution

- ▶ Scan phase
- ▶ Specialized execution phase

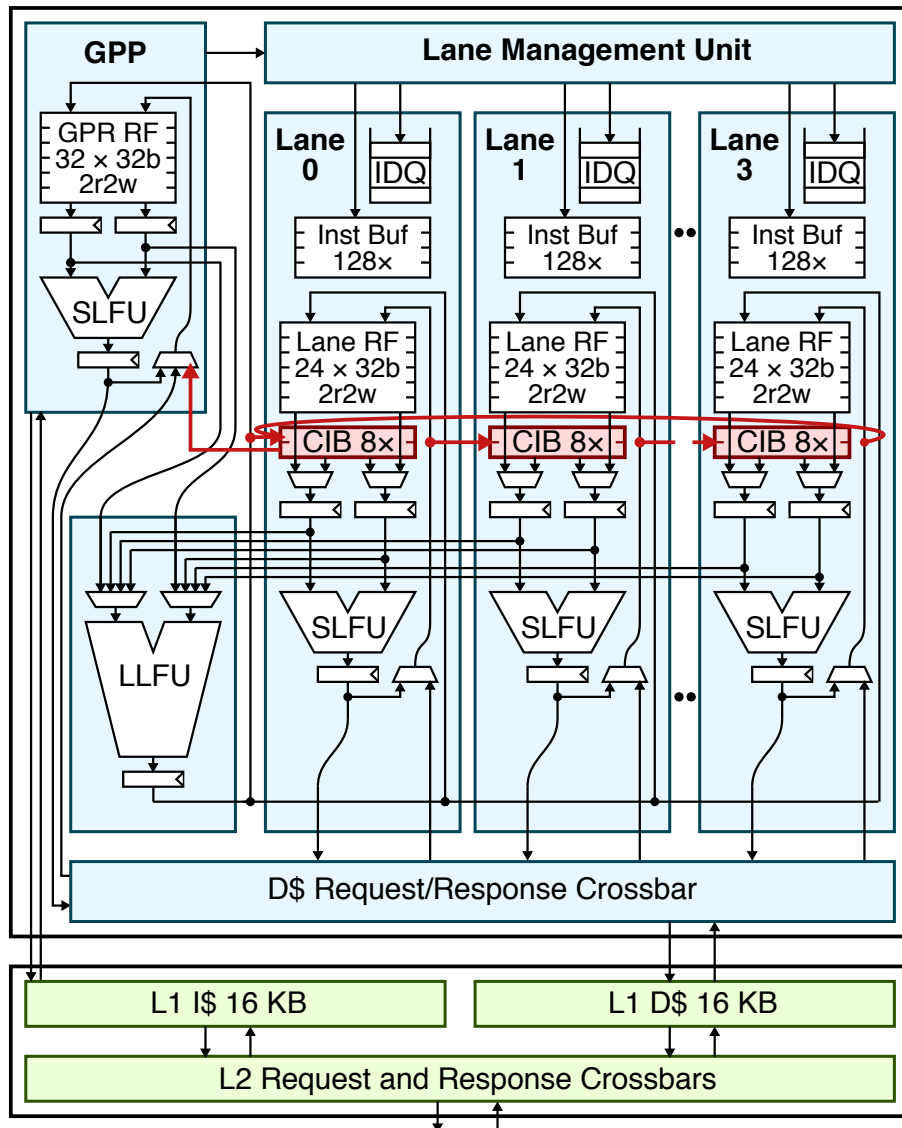
```

loop:
  lw      r2, 0(rA)
  lw      r3, 0(rB)
  mul     r4, r2, r3
  sw      r4, 0(rC)
  addiu.xi rA, 4
  addiu.xi rB, 4
  addiu.xi rC, 4
  addiu    r1, r1, 1
  xloop.uc r1, rN, loop

```

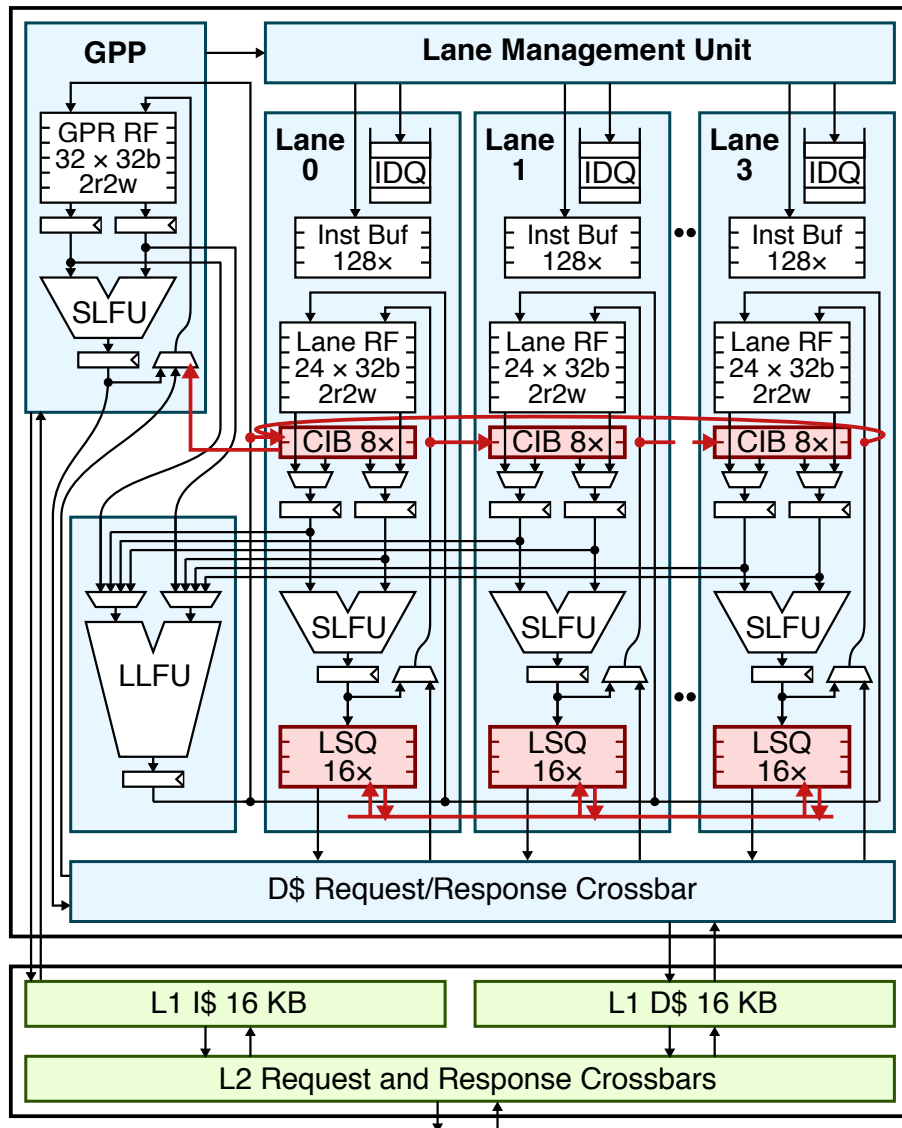


Specialized Execution – xloop.or



- ▶ **Cross-iteration buffers (CIBs)** forward register-dependences
- ▶ **LMU control logic**
 - ▷ Cross-iteration registers (CIRs)
 - ▷ Last update to a CIR
- ▶ **Lane control logic**
 - ▷ Stall if CIR is not available
 - ▷ If last update to CIR then write to the next CIB

Specialized Execution – xloop.om

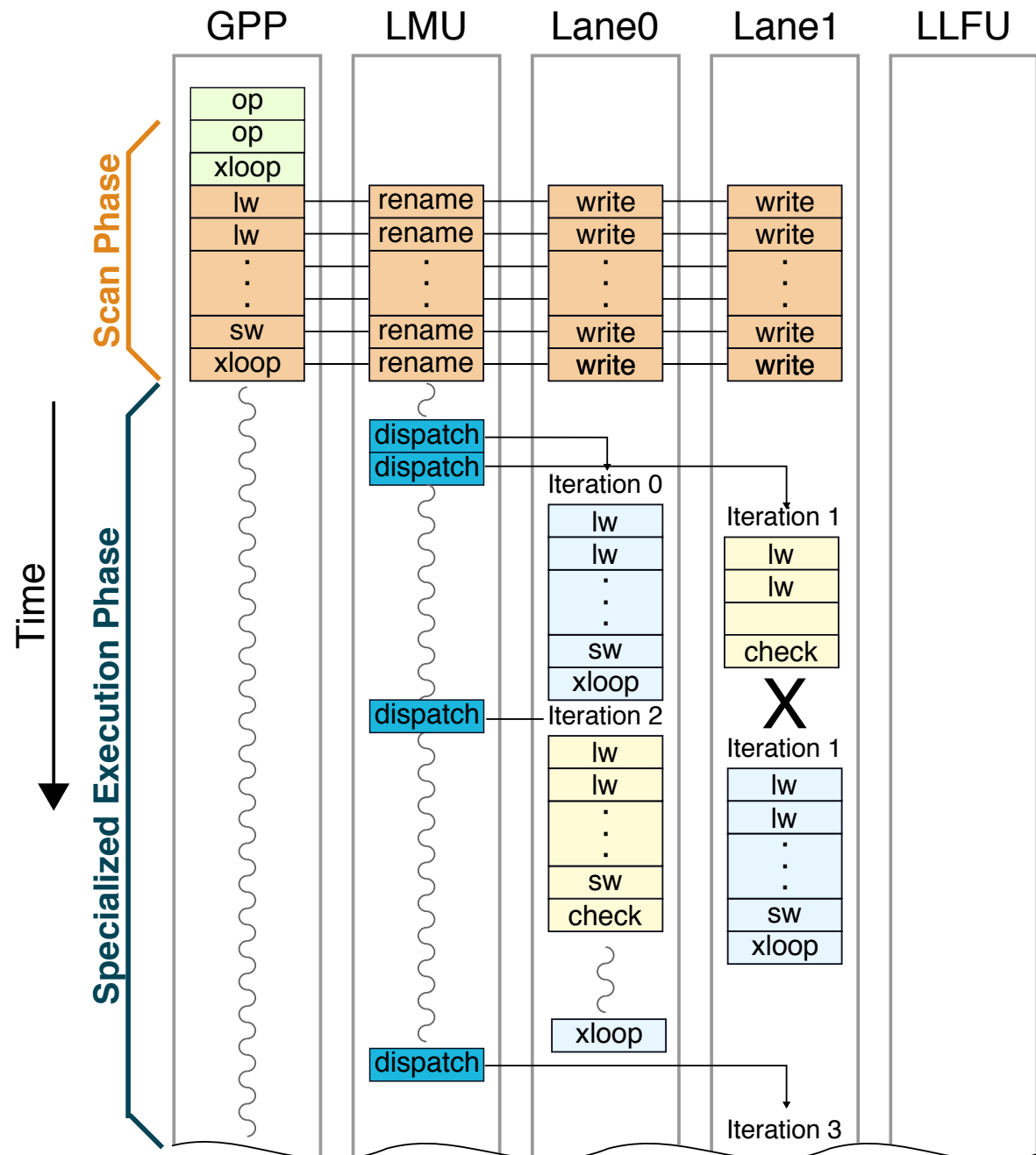


- ▶ **LSQ** to support hardware memory disambiguation
- ▶ **LMU control logic**
 - ▷ Track non-speculative vs. speculative lanes
 - ▷ Promote lanes to be non-speculative
- ▶ **Lane control logic**
 - ▷ Handle structural hazards
 - ▷ Handle dependence violations

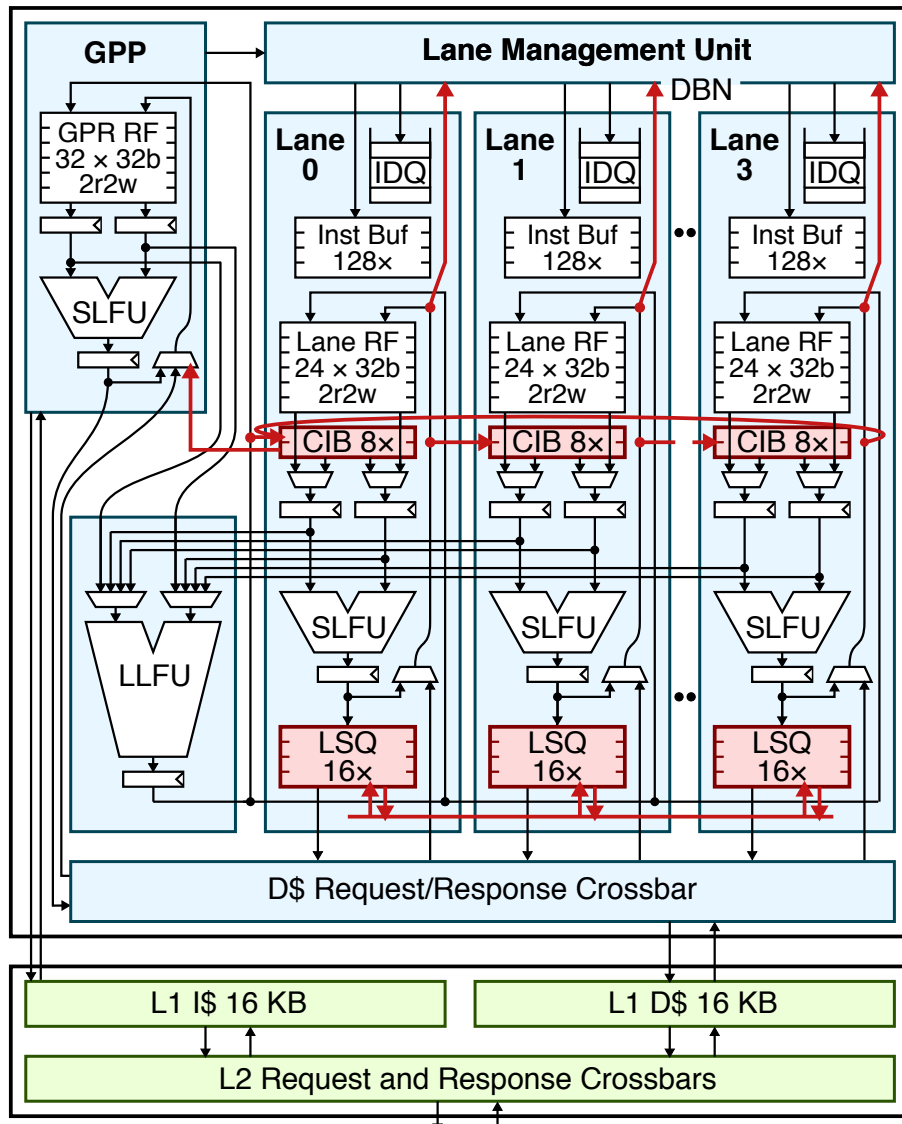
```

loop:
  lw      r4, 0(r3)
  lw      r5, 0(rA)
  ...
  ...
  sw      r6, 0(r7)
  addiu   r1, r1, 1
  xloop.om r1, rN, loop

```

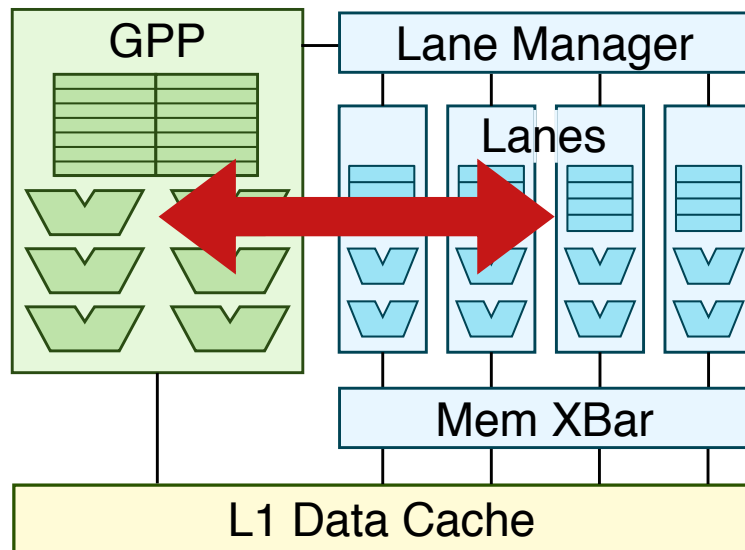


Supporting other patterns



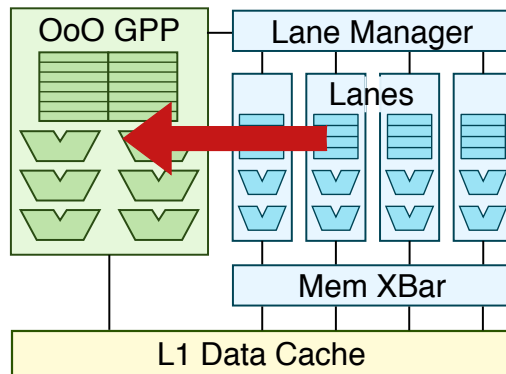
- ▶ `xloop.ua` – Using `xloop.om` mechanisms
- ▶ `xloop.orm` – Combine `xloop.or` and `xloop.om` mechanisms
- ▶ `xloop.*.db`
 - ▷ Lanes communicate updates to loop bound
 - ▷ LMU tracks maximum bound and generates additional work

Adaptive Execution

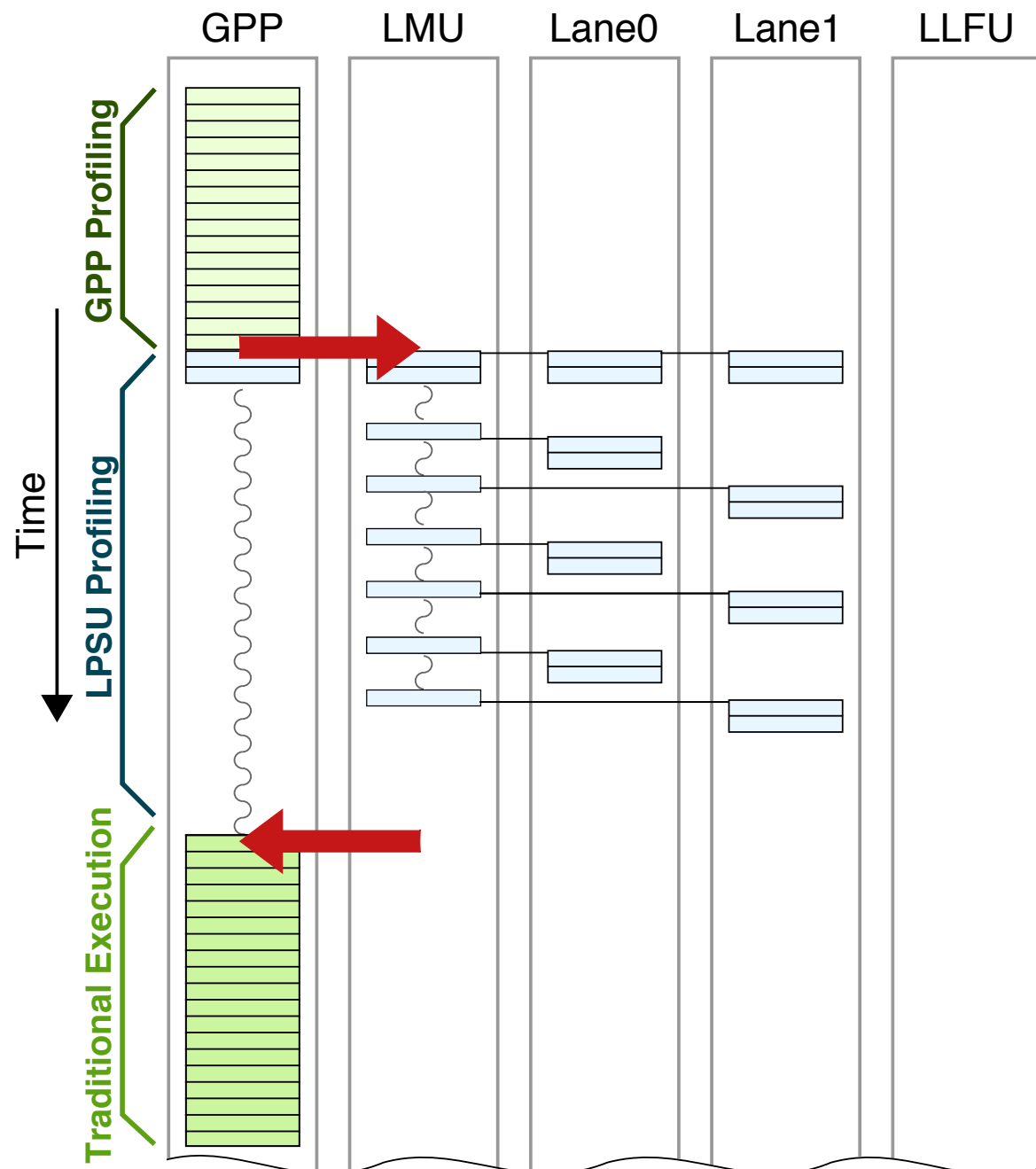


- ▶ Some kernels have higher performance on LPSU (e.g., significant inter-iteration parallelism)
- ▶ Some kernels have higher performance on GPP (e.g., limited inter-iteration parallelism, significant intra-iteration parallelism)

- ▶ **Approach #1:** Move to more complicated superscalar or out-of-order lanes to better exploit both inter- and intra-iteration parallelism
- ▶ **Approach #2:** Adaptively migrate between traditional and specialized execution to achieve best performance



- ▶ Migrating loop on iteration boundaries is very cheap and usually only requires sending the next iteration index
- ▶ An adaptive profiling table in GPP records profiling progress for small number of recently seen `xloop` instructions



1. XLOOPS Instruction Set

loop:

lw r2, 0(rA)

lw r3, 0(rB)

...

addiu.xi rA, 4

addiu.xi rB, 4

addiu r1, r1, 1

xloop.uc r1, rN, loop

2. XLOOPS Compiler

#pragma xloops ordered

for(i = 0; i < N i++)

A[i] = A[i] * A[i-K];

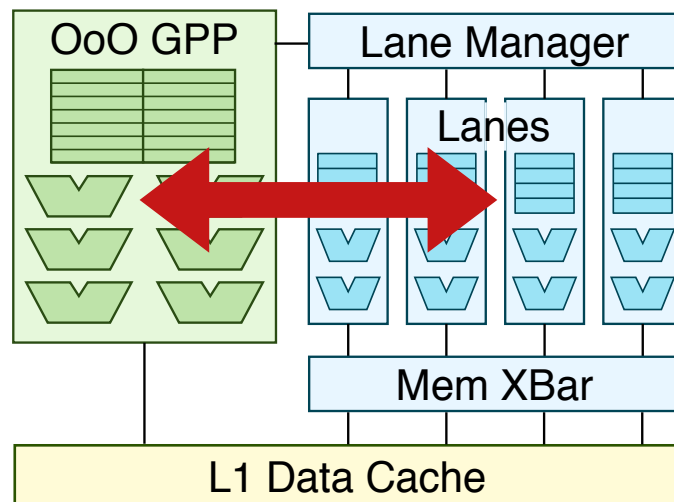
#pragma xloops atomic

for(i = 0; i < N; i++)

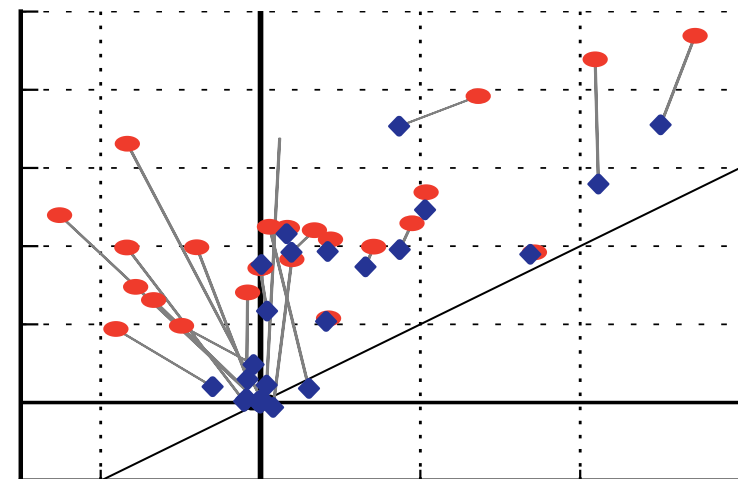
B[A[i]]++;

D[C[i]]++;

3. XLOOPS Microarchitecture



4. Evaluation



Application Kernels

xloop.uc

Color space conversion

Dense matrix-multiply

String search algorithm

Symmetric matrix-multiply

Viterbi decoding algorithm

Floyd-Warshall shortest path

xloop.om

Dynamic-programming

K-Nearest neighbors

Knapsack kernel

Floyd-Warshall shortest path

xloop.uc.db

Breadth-first search

Quick-sort algorithm

xloop.or

ADPCM decoder

Covariance computation

Floyd-Steinberg dithering

K-Means clustering

SHA-1 encryption kernel

Symmetric matrix-multiply

xloop.orm, xloop.ua

Greedy maximal-matching

2D Stencil computation

Binary tree construction

Heap-sort computation

Huffman entropy coding

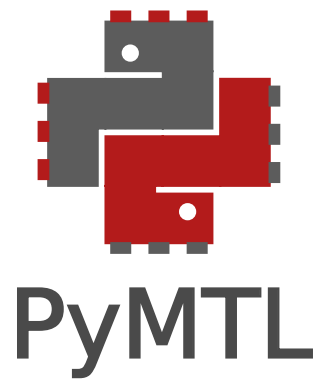
Radix sort algorithm

25 Kernels: MiBench,
PolyBench, PBBS, custom

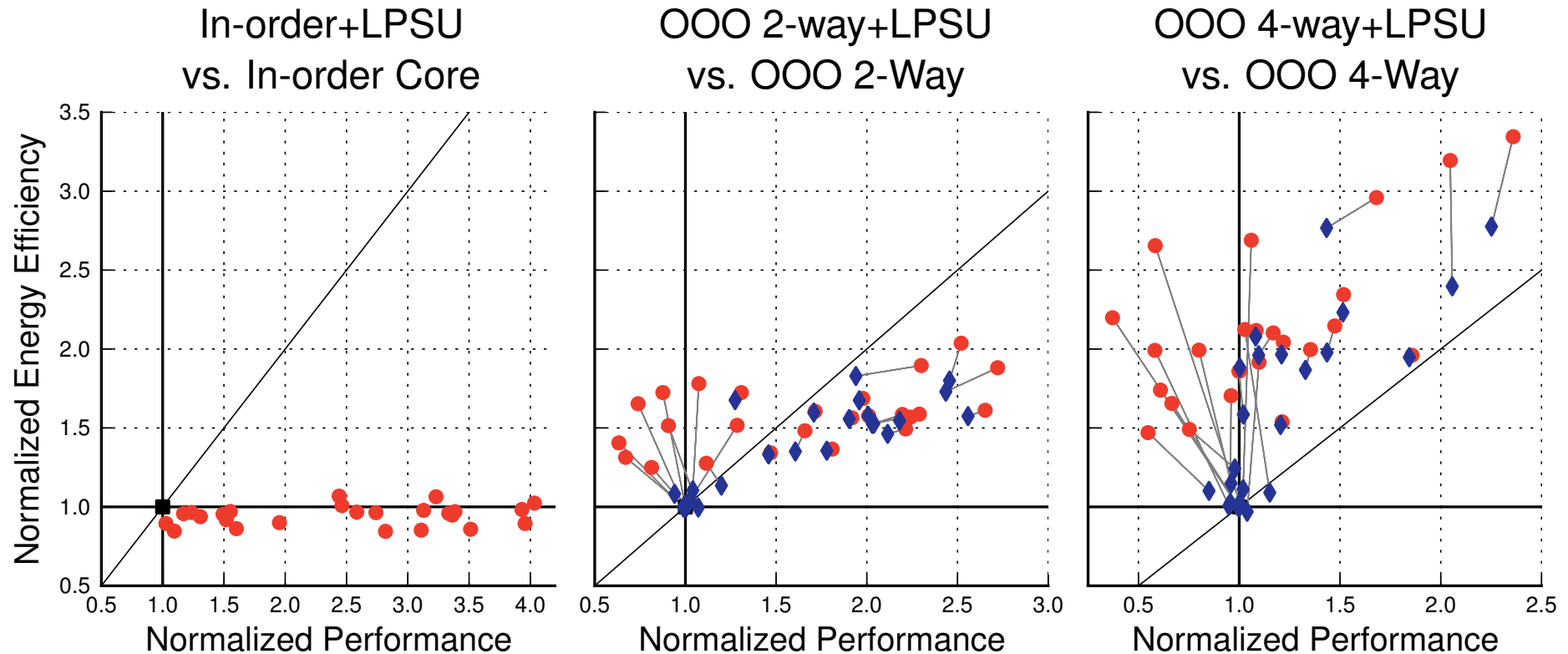
Cycle-Level Evaluation Methodology



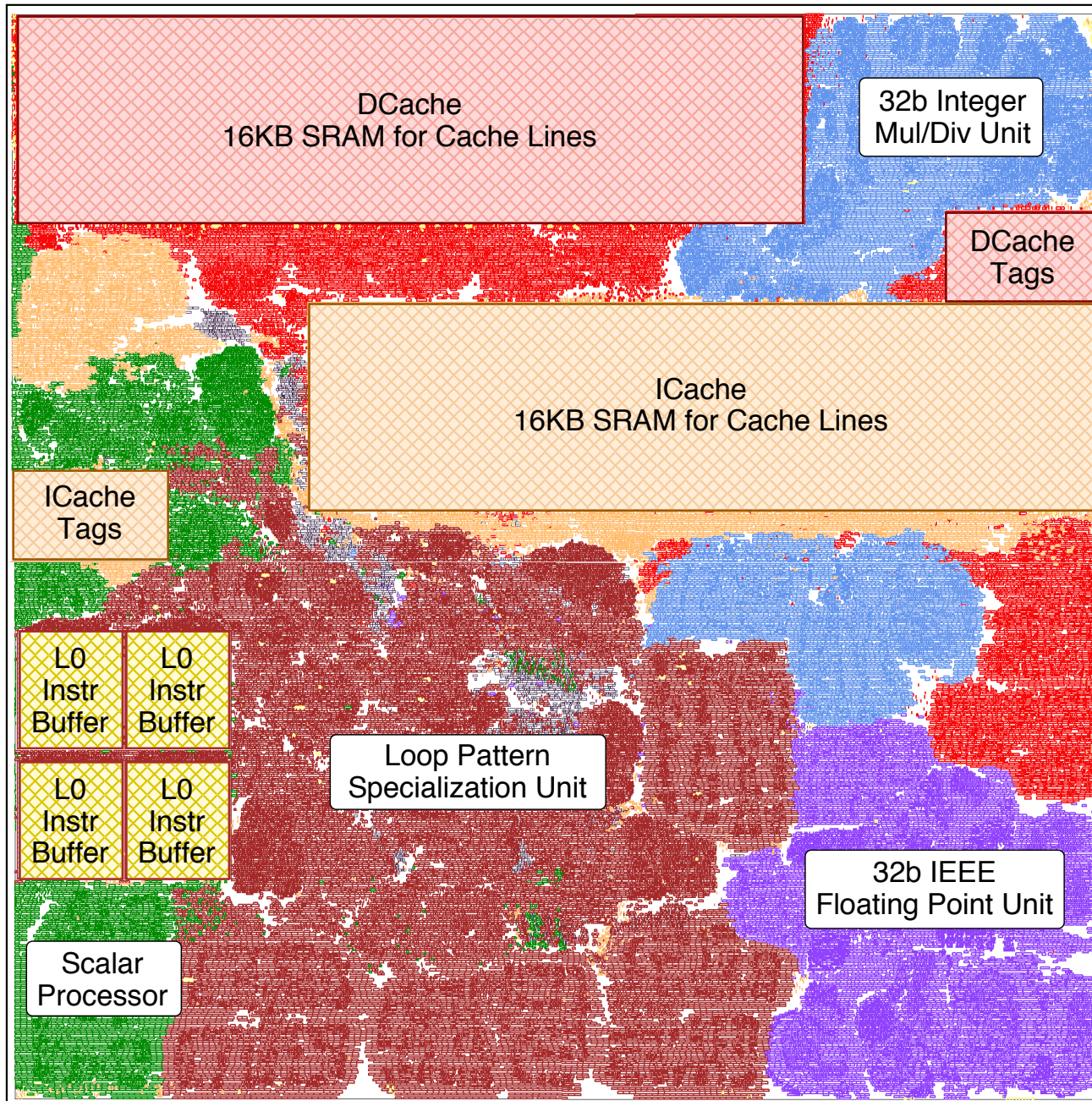
- ▶ LLVM-3.1 based compiler framework
- ▶ gem5 – in-order and out-of-order processors
- ▶ PyMTL – LPSU models
- ▶ McPAT-1.0 – 45nm energy models



Energy-Efficiency vs. Performance Results



- ▶ XLOOPS vs. Simple Core : Similar energy efficiency, higher power
- ▶ XLOOPS vs. OOO 2-way : Higher energy efficiency, mixed power
- ▶ XLOOPS vs. OOO 4-way : Higher energy efficiency, lower power
- ▶ Adaptive execution trades energy efficiency for performance
- ▶ Profiling and migration cause minimal performance degradation



VLSI Implementation

- ▶ TSMC 40 nm standard-cell-based implementation
- ▶ RISC scalar processor with 4-lane LPSU
- ▶ Supports `xloop.uc`
- ▶ $\approx 40\%$ extra area compared to simple RISC processor

```

loop:
  lw      r2, 0(rA)
  lw      r3, 0(rB)
  ...
  addiu.xi rA, 4
  addiu.xi rB, 4
  addiu   r1, r1, 1
  xloop.uc r1, rN, loop

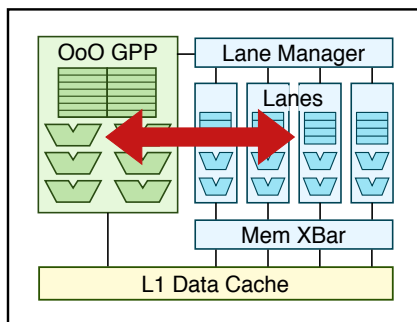
```

```

#pragma xloops ordered
for(i = 0; i < N i++)
  A[i] = A[i] * A[i-K];

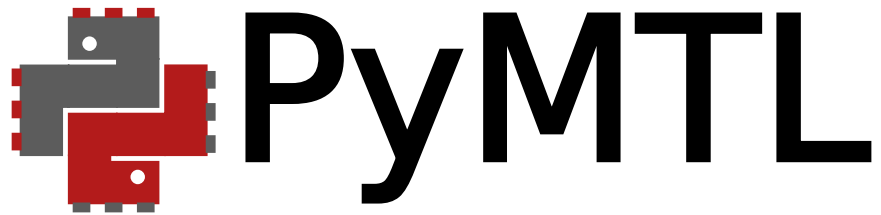
#pragma xloops atomic
for(i = 0; i < N; i++)
  B[ A[i] ]++;
  D[ C[i] ]++;

```



XLOOPS Take-Away Points

- ▶ XLOOPS is an elegant new abstraction that enables performance-portable execution of loops
- ▶ XLOOPS enables a single-ISA heterogeneous architecture with a new execution paradigm
 - ▷ Traditional Execution
 - ▷ Specialized Execution
 - ▷ Adaptive Execution
- ▶ XLOOPS is able to achieve higher performance compared to simple in-order cores and improved energy efficiency compared to complex out-of-order cores



PyMTL: A Unified Framework for
Vertically Integrated Computer
Architecture Research

Derek Lockhart, Gary Zibrat,
Christopher Batten

47th ACM/IEEE Int'l Symp. on
Microarchitecture (MICRO)
Cambridge, UK, Dec. 2014

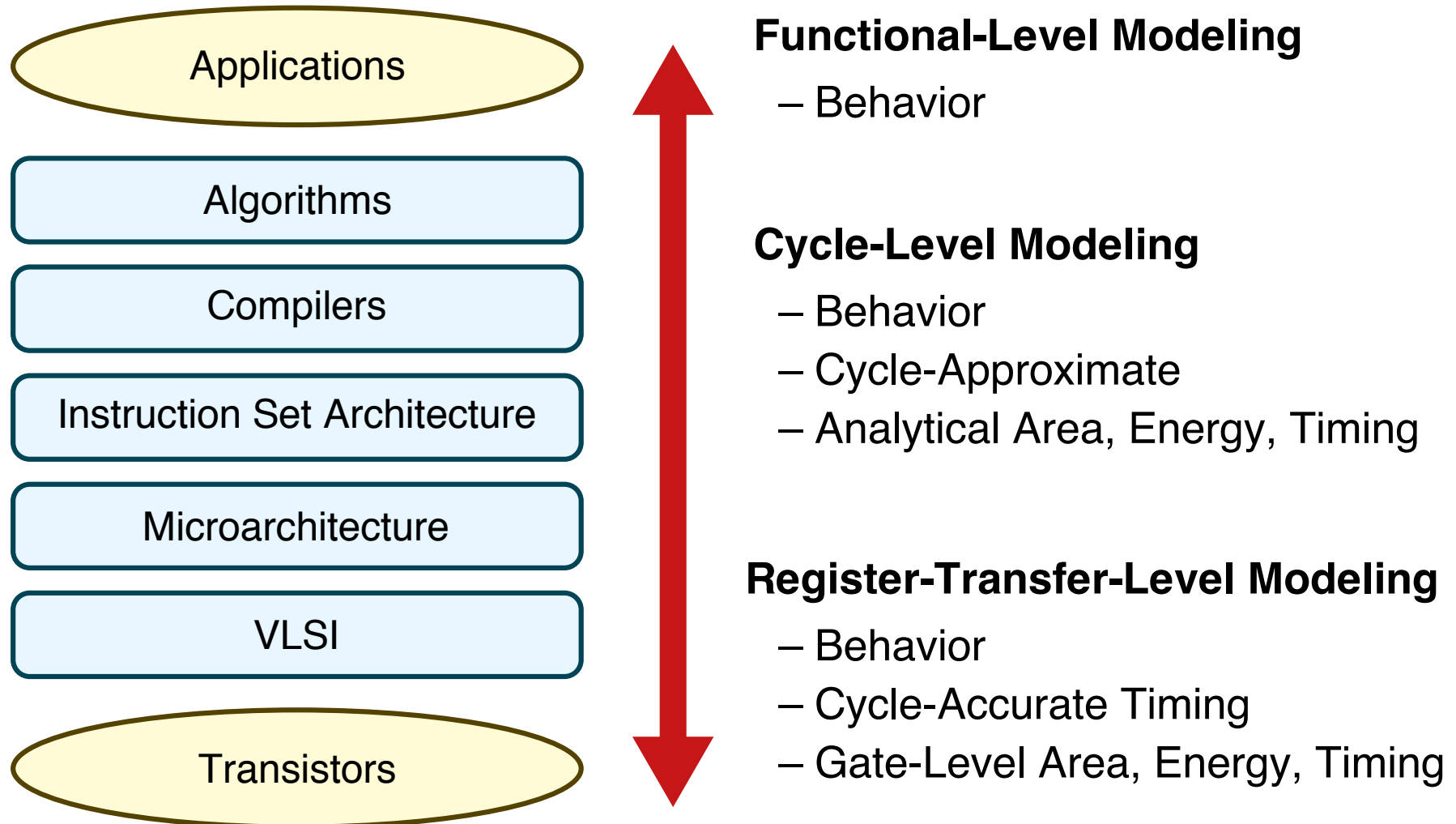


Pydgin: Generating Fast
Instruction Set Simulators from
Simple Architecture Descriptions
with Meta-Tracing JIT Compilers

Derek Lockhart, Berkin Ilbeyi,
Christopher Batten

IEEE Int'l Symp. on Perf Analysis of
Systems and Software (ISPASS)
Philadelphia, NJ, Mar. 2015

Computer Architecture Research Methodologies



Computer Architecture Research Methodologies

Computer Architecture Research Methodology Gap

FL, CL, RTL modeling
use very different
languages, patterns,
tools, and methodologies



Functional-Level Modeling

- Algorithm/ISA Development
- MATLAB/Python, C++ ISA Sim

Cycle-Level Modeling

- Design-Space Exploration
- C++ Simulation Framework
- SW-Focused Object-Oriented
- gem5, SESC, McPAT

Register-Transfer-Level Modeling

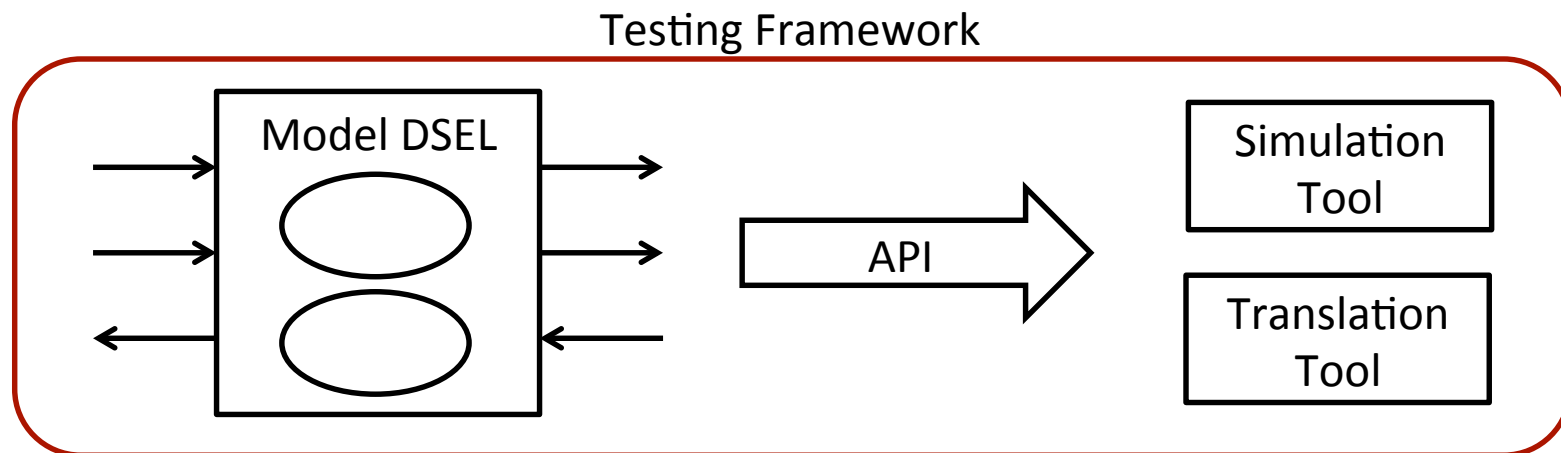
- Prototyping & AET Validation
- Verilog, VHDL Languages
- HW-Focused Concurrent Structural
- EDA Toolflow

Great Ideas From Prior Work

- **Concurrent-Structural Modeling**
(Liberty, Cascade, SystemC) Consistent interfaces across abstractions
- **Unified Modeling Languages**
(SystemC) Unified design environment for FL, CL, RTL
- **Hardware Generation Languages**
(Chisel, Genesis2, BlueSpec, MyHDL) Productive RTL design space exploration
- **HDL-Integrated Simulation Frameworks**
(Cascade) Productive RTL validation and cosimulation
- **Latency-Insensitive Interfaces**
(Liberty, BlueSpec) Component and test bench reuse

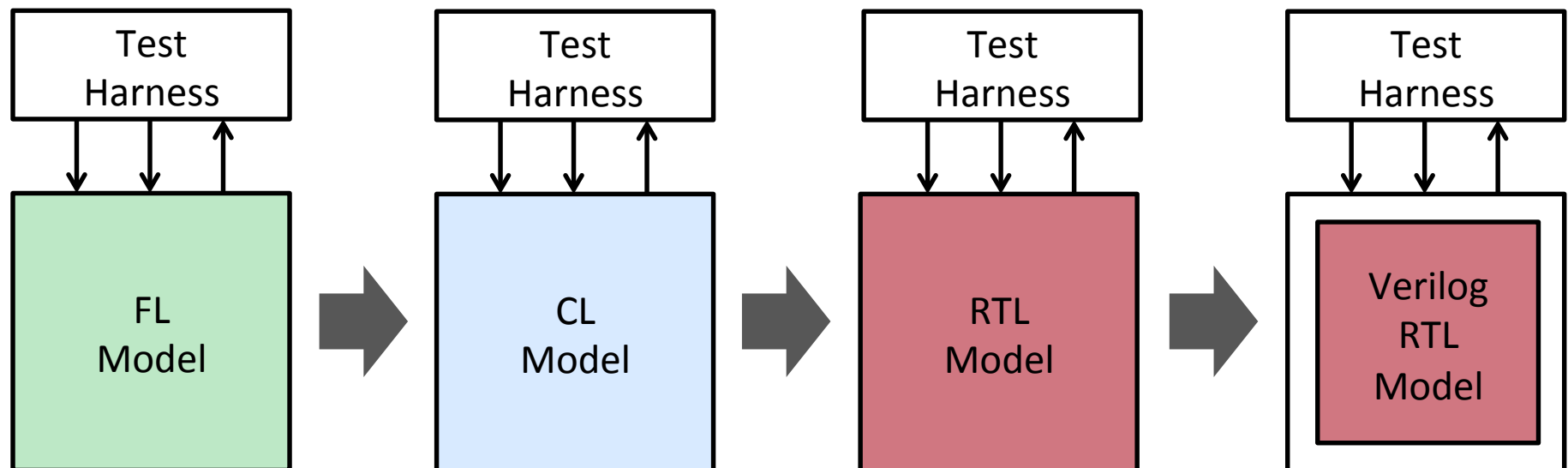
What is PyMTL?

- A Python DSEL for concurrent-structural hardware modeling
- A Python API for analyzing models described in the PyMTL DSEL
- A Python tool for simulating PyMTL FL, CL, and RTL models
- A Python tool for translating PyMTL RTL models into Verilog
- A Python testing framework for model validation



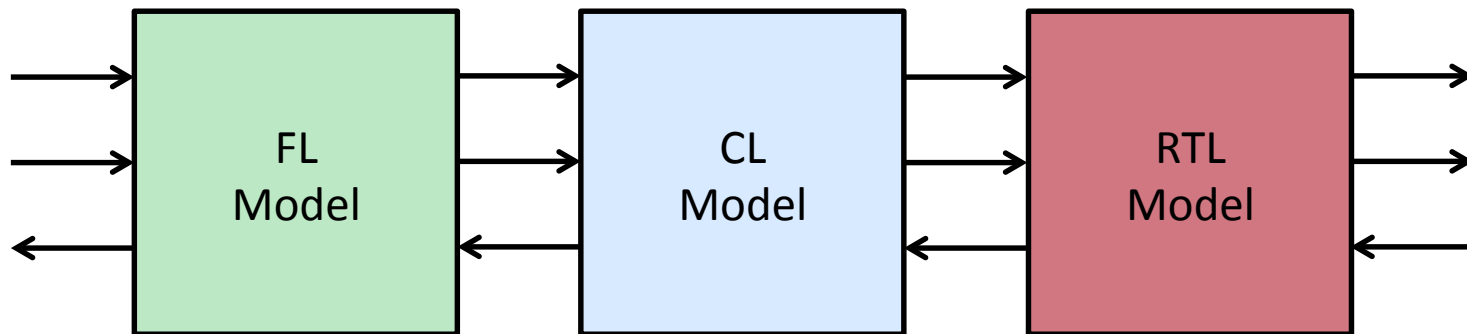
What Does PyMTL Enable?

- Incremental refinement from algorithm to accelerator implementation
- Automated testing and integration of PyMTL-generated Verilog



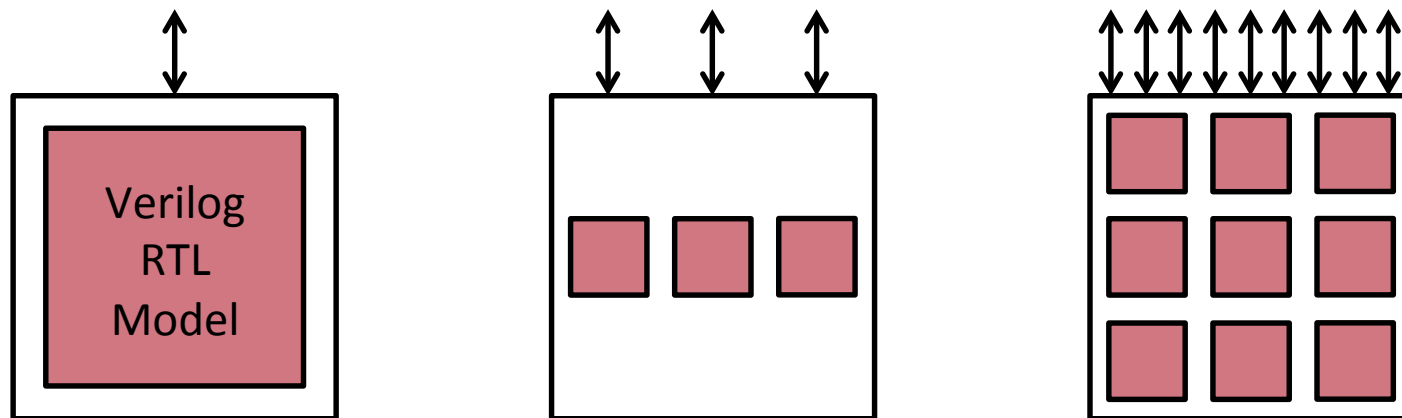
What Does PyMTL Enable?

- Incremental refinement from algorithm to accelerator implementation
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- Multi-level co-simulation of FL, CL, and RTL models



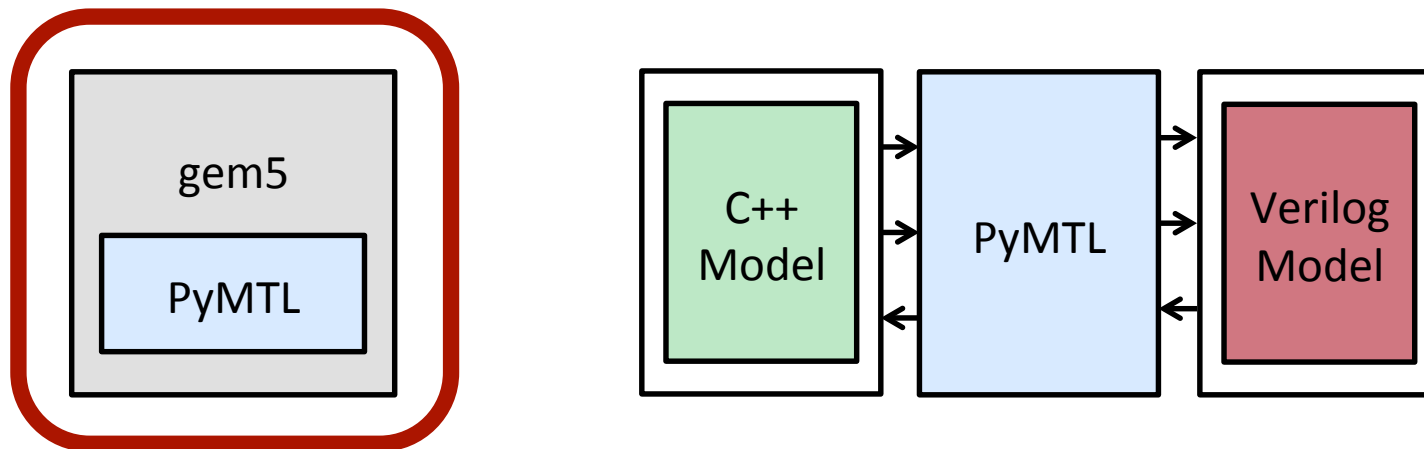
What Does PyMTL Enable?

- Incremental refinement from algorithm to accelerator implementation
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- Multi-level co-simulation of FL, CL, and RTL models
- Construction of highly-parameterized RTL chip generators

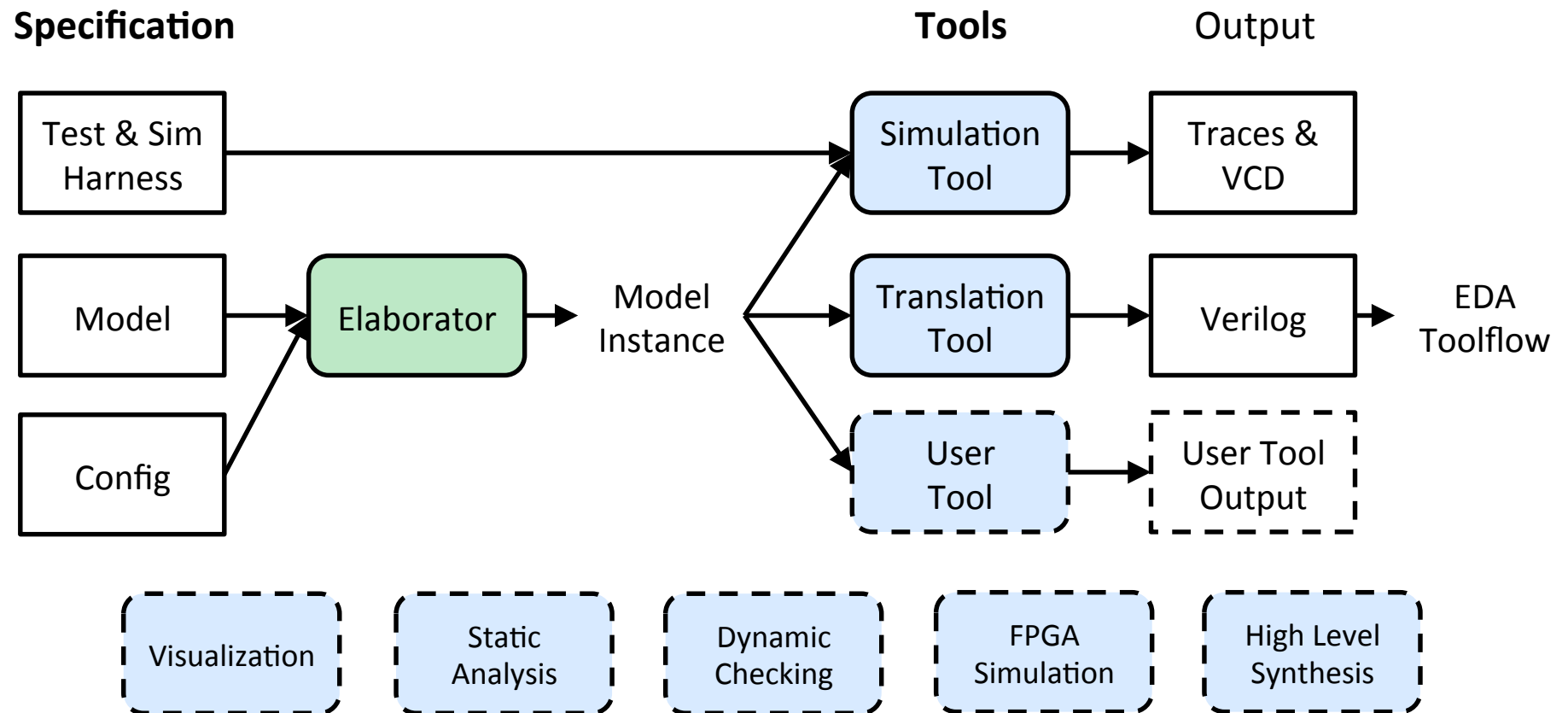


What Does PyMTL Enable?

- Incremental refinement from algorithm to accelerator implementation
- Automated testing and integration of PyMTL-generated Verilog
- Multi-level co-simulation of FL, CL, and RTL models
- Construction of highly-parameterized RTL chip generators
- Embedding within C++ frameworks & integration of C++/Verilog models
(Used to implement CL model for XLOOPS LPSU)



The PyMTL Framework

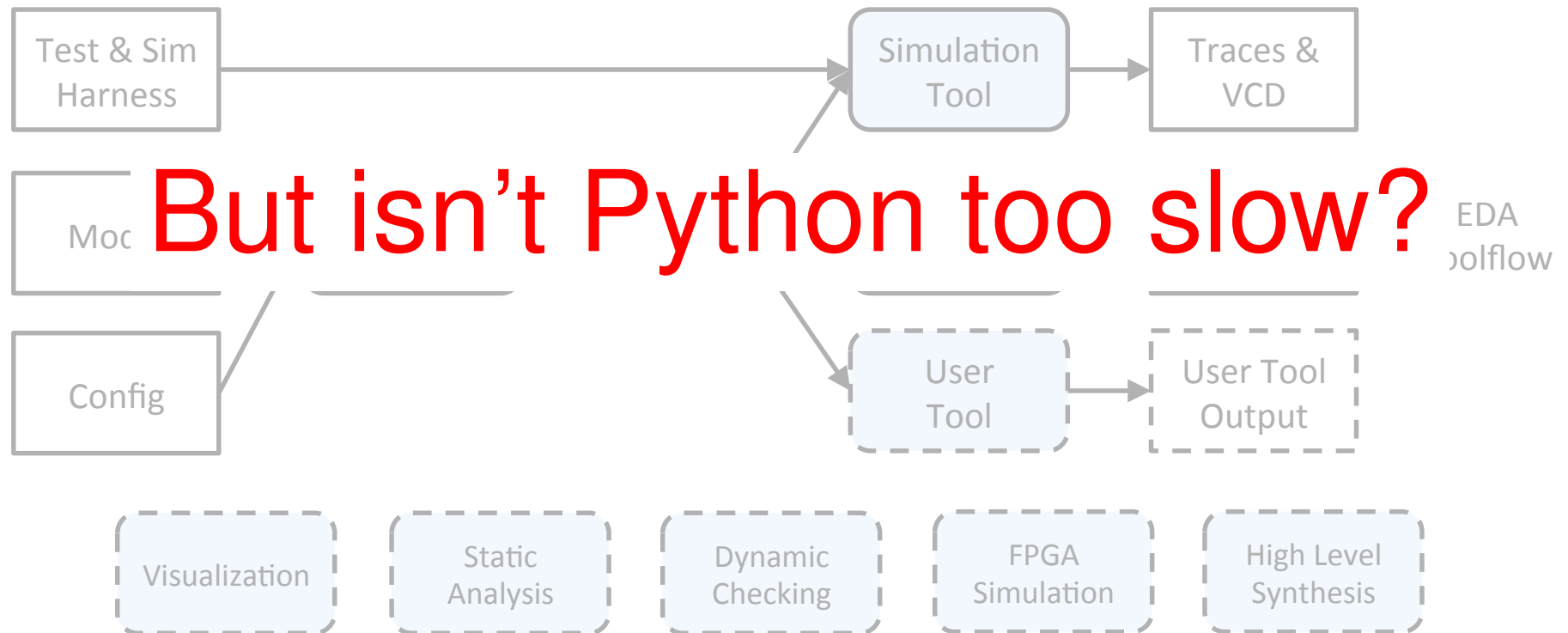


The PyMTL Framework

Specification

Tools

Output

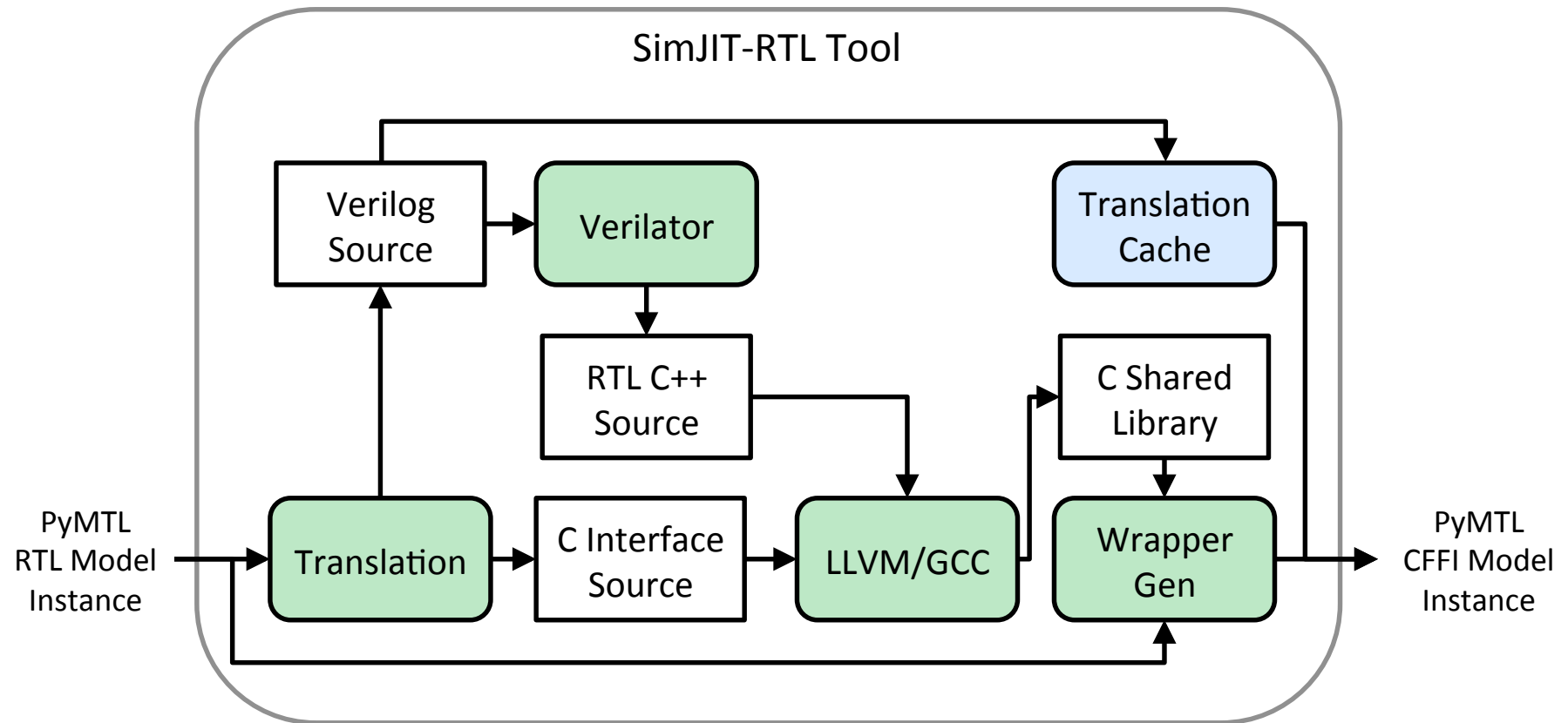


Performance/Productivity Gap

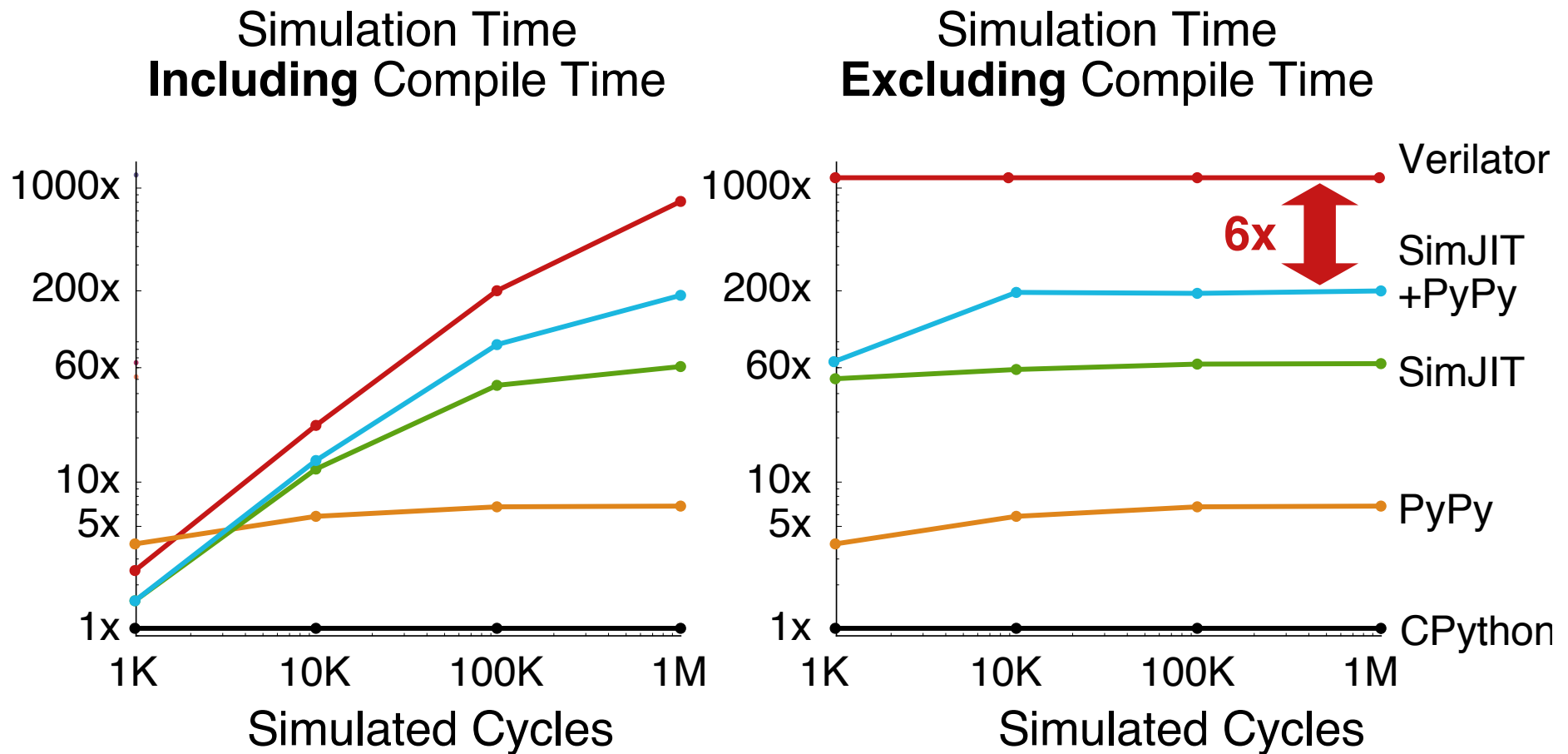
Python is growing in popularity in many domains of scientific and high-performance computing. **How do they close this gap?**

- ▶ Python-Wrapped C/C++ Libraries
(NumPy, CVXOPT, NLPy, pythonoCC, gem5)
- ▶ Numerical Just-In-Time Compilers
(Numba, Parakeet)
- ▶ Just-In-Time Compiled Interpreters
(PyPy, Pyston)
- ▶ Selective Embedded Just-In-Time Specialization
(SEJITS)

PyMTL SimJIT-RTL Architecture

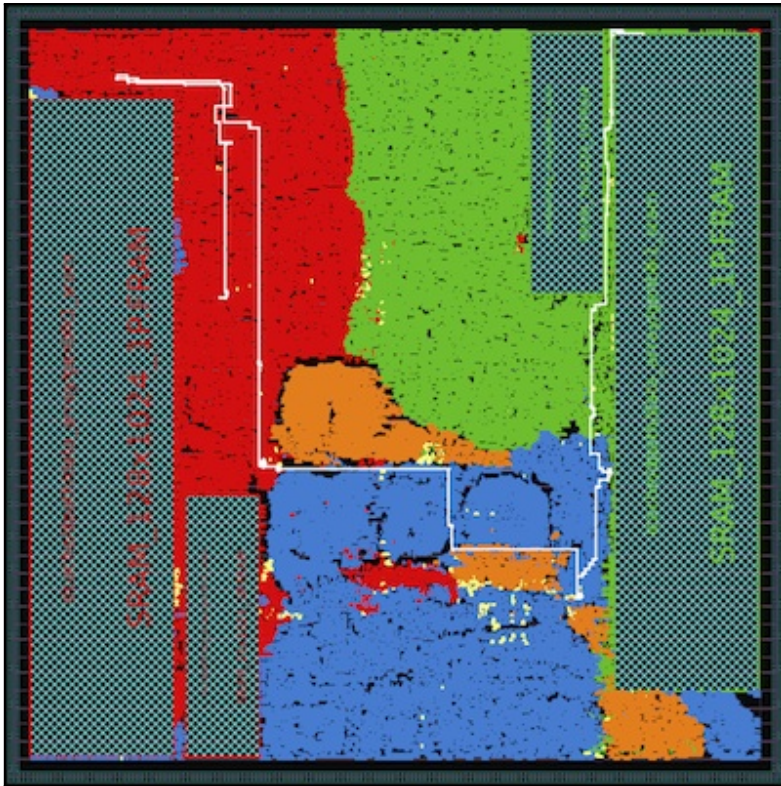


PyMTL Results: 64-Node Mesh Network



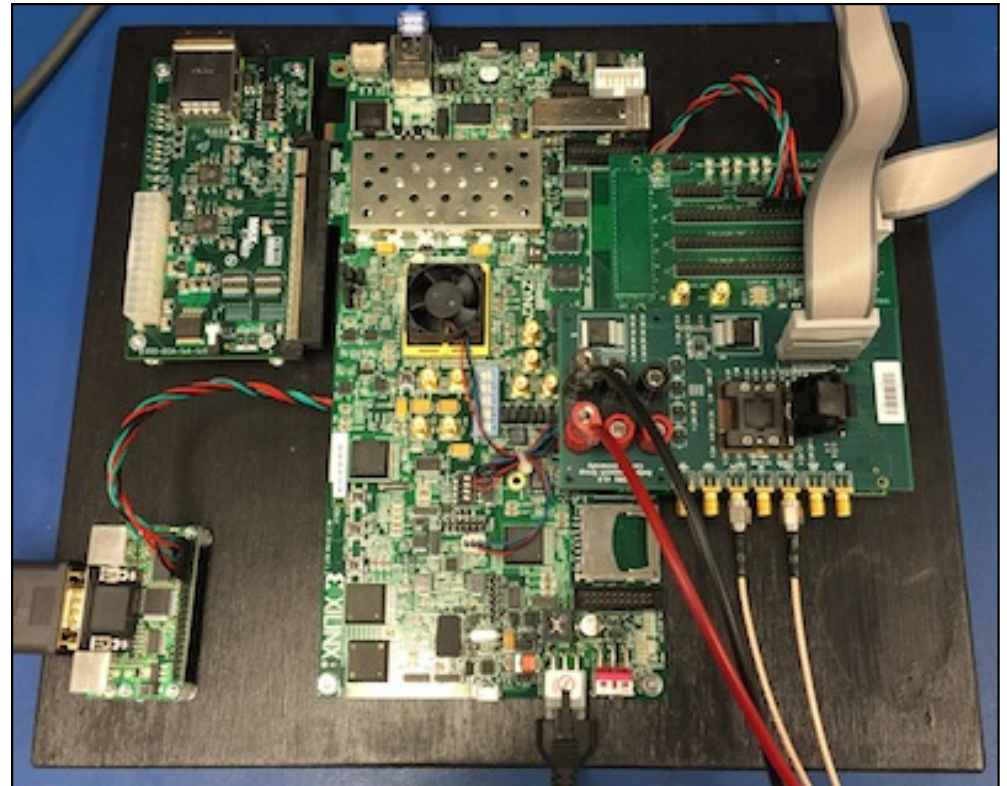
RTL model of 64-node mesh network with single-cycle routers, elastic buffer flow control, uniform random traffic, with an injection rate just before saturation

PyMTL ASIC Tapeout



Layout generated from PyMTL for
simple processor, L1 memory
system, dot product xcel

Target Tech: 2x2mm IBM 130nm



Xilinx ZC706 FPGA development board
for FPGA prototyping

Custom designed FMC mezzanine card
for ASIC test chips



PyMTL: A Unified Framework for
Vertically Integrated Computer
Architecture Research

Derek Lockhart, Gary Zibrat,
Christopher Batten

47th ACM/IEEE Int'l Symp. on
Microarchitecture (MICRO)
Cambridge, UK, Dec. 2014



Pydgin: Generating Fast
Instruction Set Simulators from
Simple Architecture Descriptions
with Meta-Tracing JIT Compilers

Derek Lockhart, Berkin Ilbeyi,
Christopher Batten

IEEE Int'l Symp. on Perf Analysis of
Systems and Software (ISPASS)
Philadelphia, NJ, Mar. 2015

Computer Architecture Research Methodologies

While it is certainly possible to create stand-alone instruction set simulators in PyMTL, their performance is quite slow (~100 KIPS)

Can we achieve high-performance while maintaining productivity for instruction set simulators?



Functional-Level Modeling

- Algorithm/ISA Development
- MATLAB/Python, C++ ISA Sim

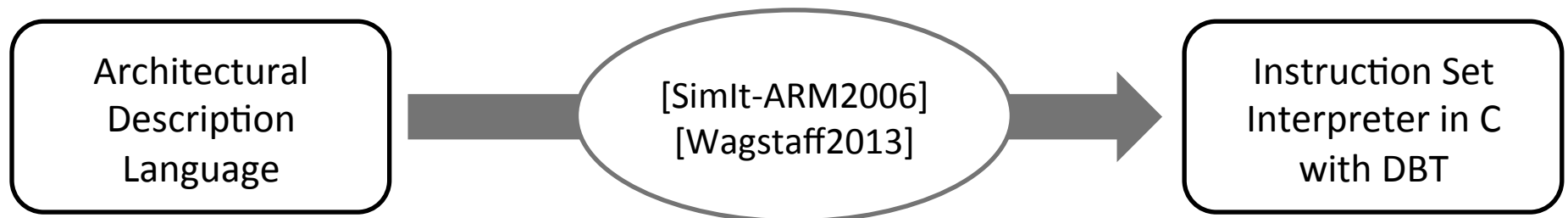
Cycle-Level Modeling

- Design-Space Exploration
- C++ Simulation Framework
- SW-Focused Object-Oriented
- gem5, SESC, McPAT

Register-Transfer-Level Modeling

- Prototyping & AET Validation
- Verilog, VHDL Languages
- HW-Focused Concurrent Structural
- EDA Toolflow

Productivity  Performance



[Simit-ARM2006]

- + Page-based JIT
- Ad-hoc ADL with custom parser
- Unmaintained

[Wagstaff2013]

- + Region-based JIT
- + Industry-supported ADL (ArchC)
- C++-based ADL is verbose
- Not Public

[Simit-ARM2006] J.D'Errico and W.Qin. Constructing Portable Compiled Instruction-Set Simulators — An ADL-Driven Approach. DATE'06.

[Wagstaff2013] H. Wagstaff, M. Gould, B. Franke, and N.Topham. Early Partial Evaluation in a JIT-Compiled, Retargetable Instruction Set Simulator Generated from a High-Level Architecture Description. DAC'13.

Productivity



Performance

Architectural
Description
Language

[SimIt-ARM2006]
[Wagstaff2013]

Instruction Set
Interpreter in C
with DBT

Key Insight:

Similar productivity-performance challenges for
building high-performance interpreters of
dynamic languages.
(e.g. JavaScript, Python)



Dynamic Language
Interpreter in C
with JIT Compiler

Productivity



Performance

Architectural
Description
Language

[SimIt-ARM2006]
[Wagstaff2013]

Instruction Set
Interpreter in C
with DBT

Dynamic-Language
Interpreter
in RPython

RPython
Translation
Toolchain



Dynamic Language
Interpreter in C
with JIT Compiler

Meta-Tracing JIT:
makes JIT generation generic across languages

Productivity



Performance

Architectural
Description
Language



Instruction Set
Interpreter in C
with DBT

RPython
Translation
Toolchain

Productivity



Performance

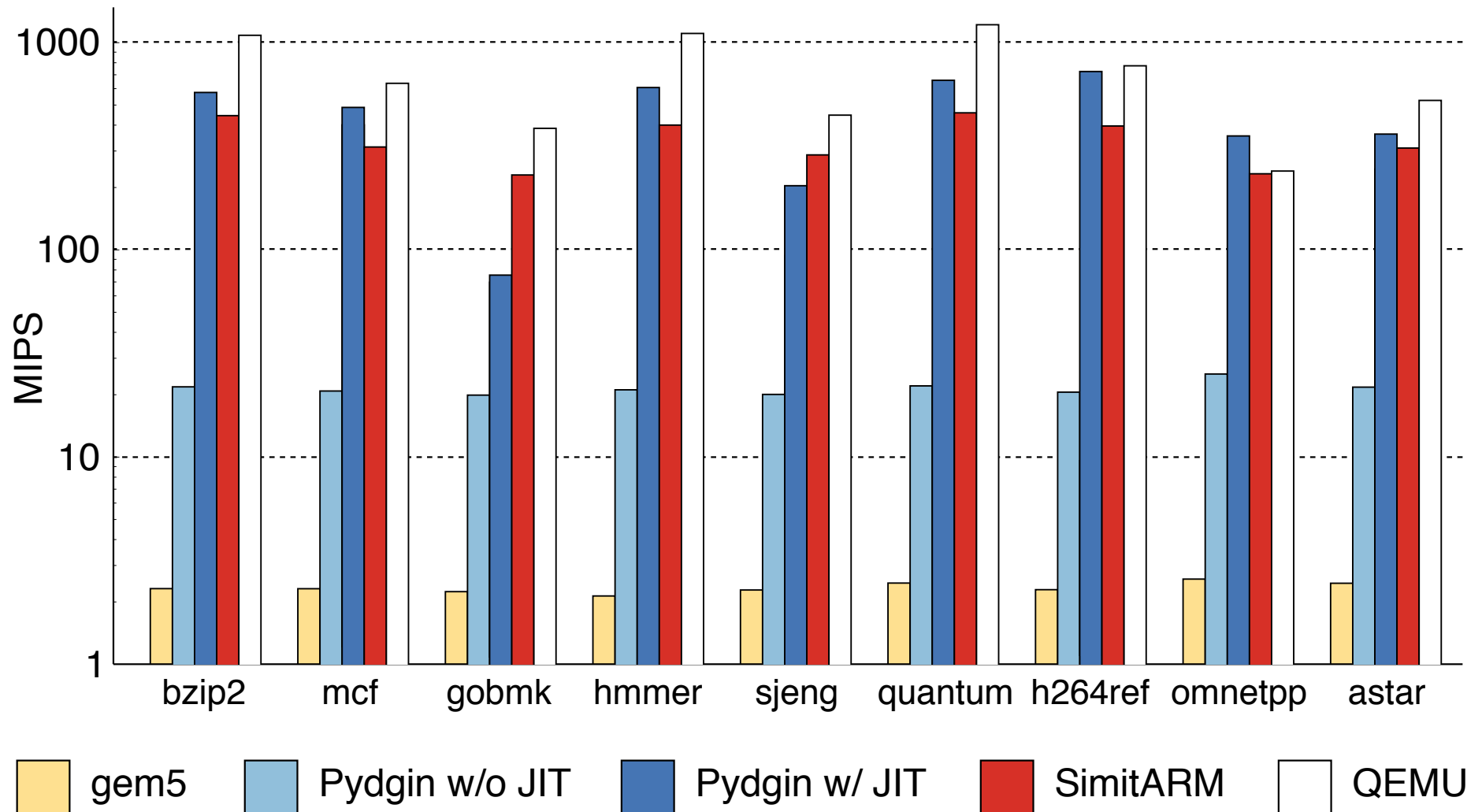
Architectural
Description
Language



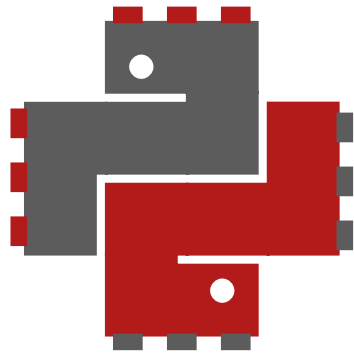
Instruction Set
Interpreter in C
with DBT

- Flexible, productive, pseudocode-like ADL syntax
- ADL embedded in a popular, general-purpose language
- Tracing-JIT generator applies across many different ISAs
- Leverages advancements from dynamic-language JIT research

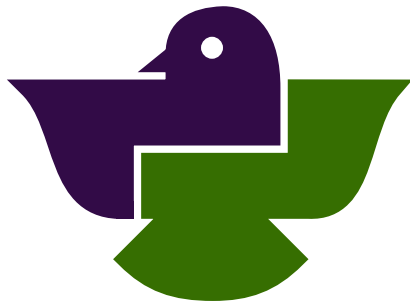
Pydgin Results: ARMv5 Instruction Set



Porting Pydgin to a new user-level ISA takes just a few weeks



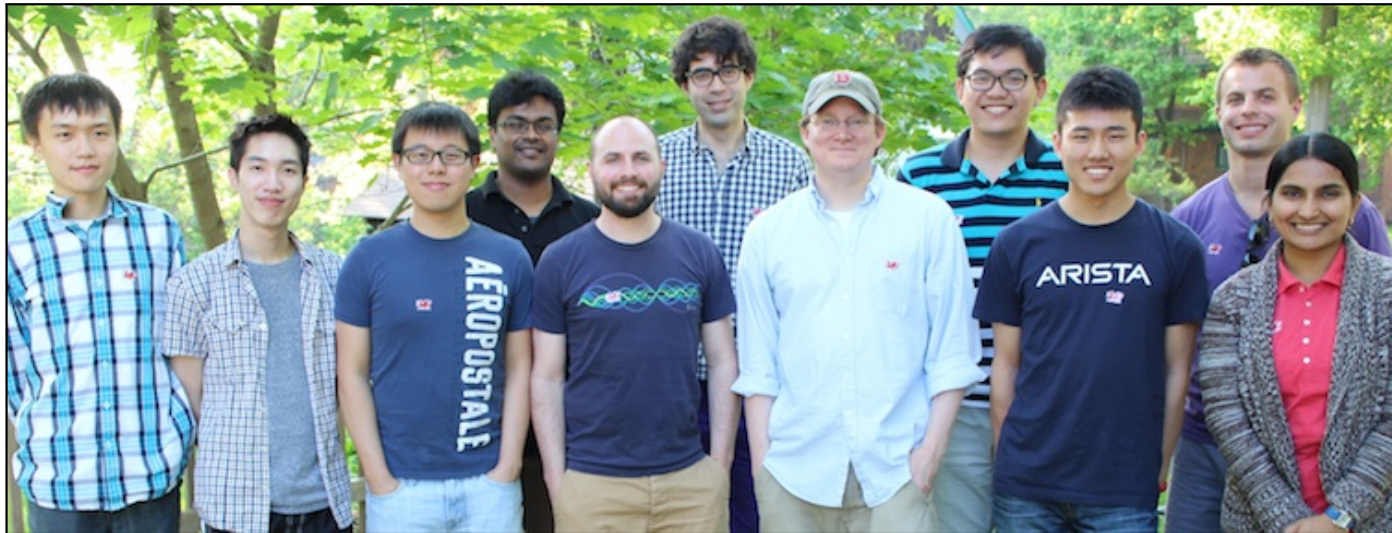
PyMTL



Pydgin

PyMTL/Pydgin Take-Away Points

- ▶ PyMTL is a productive Python framework for FL, CL, and RTL modeling and hardware design
- ▶ Pydgin is a framework for rapidly developing very fast instruction-set simulators from a Python-based architecture description language
- ▶ PyMTL and Pydgin leverage novel application of JIT compilation to help close the performance/productivity gap
- ▶ Alpha versions of PyMTL and Pydgin are available for researchers to experiment with at <https://github.com/cornell-brg/pymtl>
<https://github.com/cornell-brg/pydgin>



Derek Lockhart, Ji Kim, Shreesha Srinath, Christopher Torng,
Berkin Ilbeyi, Moyang Wang, and many M.S./B.S. students

Prof. Zhiru Zhang, Mingxing Tan, Gai Liu



Equipment and Tool Donations
Intel, NVIDIA, Synopsys, Xilinx

Batten Research Group

Exploring cross-layer hardware specialization using a vertically integrated research methodology

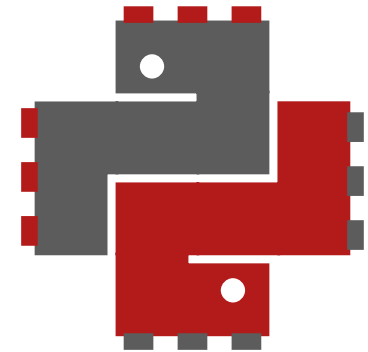
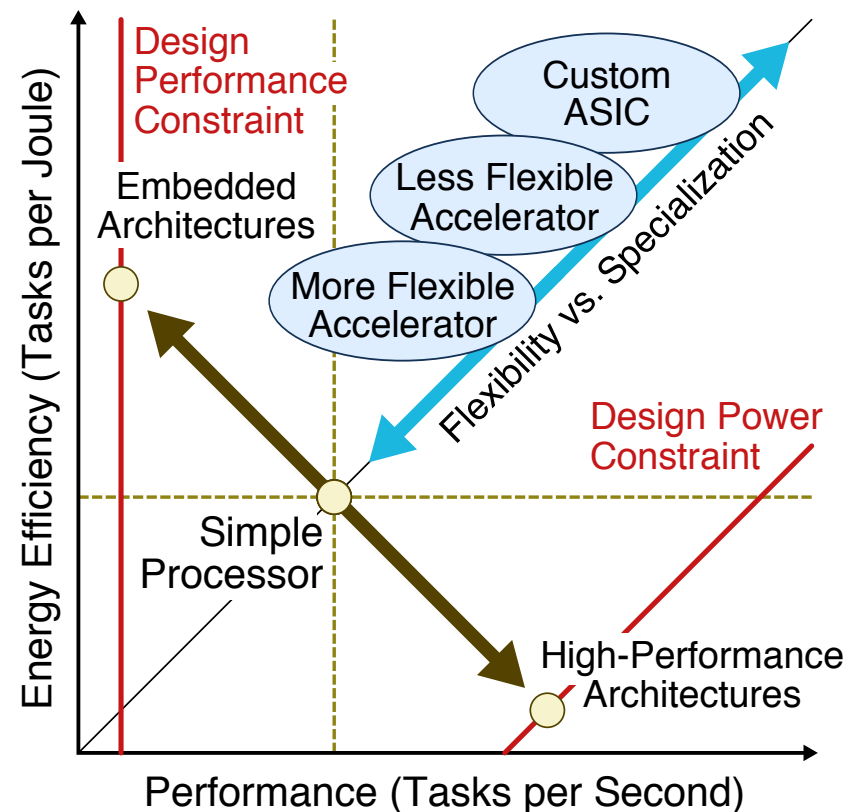
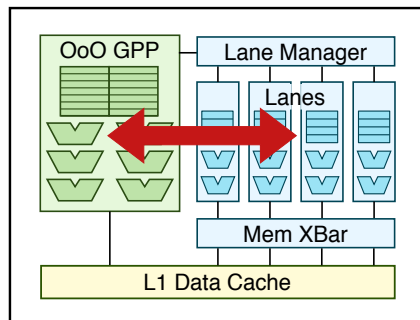
```

loop:
  lw      r2, 0(rA)
  lw      r3, 0(rB)
  ...
  addiu.xi rA, 4
  addiu.xi rB, 4
  addiu    r1, r1, 1
  xloop.uc r1, rN, loop
  
```

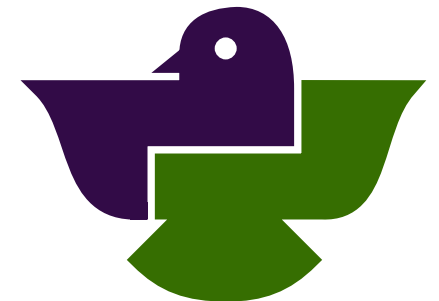
```

#pragma xloops ordered
for(i = 0; i < N i++)
  A[i] = A[i] * A[i-K];

#pragma xloops atomic
for(i = 0; i < N; i++)
  B[ A[i] ]++;
  D[ C[i] ]++;
  
```



PyMTL



Pydgin